fundamental interactions

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FUNDAMENTAL FORCES

force	range	strength	acts on
gravity	∞	$G_{Newton} \approx 6 \times 10^{-39}$	all [massive] particles
weak [nuclear]	<10 ⁻¹⁸ m	$G_{Fermi} \approx 1 \times 10^{-5}$	leptons, hadrons
electromagnetism	∞	<i>α</i> =1/137	all charged particles
strong [nuclear]	$\approx 1 \times 10^{-15} \text{ m}$	$g^2 \approx 1$	hadrons

- all natural phenomena result from the effect of just four fundamental forces [the unifying power of Physics]
- all phenomena experienced in everyday life are explained by just two: gravity and electromagnetism [those with infinite range]

[DISCLAIMER] I WILL NOT TALK ABOUT GRAVITY

- gravity will be conspicuously absent from my discussion
 - I will only discuss physics at scales [small yet sufficiently large] and for masses [small] for which gravity effects are negligible
 - I will focus on quantum descriptions of fundamental interactions
 - a consistent quantum theory of gravity remains elusive

[José Sande Lemos, Thu & Fri & Sat]

ELECTROMAGNETISM

- in the classical regime all electromagnetic phenomena are described by Maxwell's equations
 - can calculate, for example, electric field due to a given configuration of charges; the wave equation for propagation of electric and magnetic fields through space; ...
 - the concept of field appears naturally
- the extension of electromagnetism to the quantum level requires that we describe the interactions of charged particles via the electromagnetic field as exchanges of quanta of the field [photons] between the particles involved [we will get to this]

A NOTE ON NATURAL UNITS

- particle physics [study of elementary particles and their interactions] uses a fit-for-purpose system of units, so-called natural, where $\hbar = c = k_B = 1$
- the fundamental unit is chosen to be the electron-volt, defined as the energy of an electron that has been accelerated through a potential difference of one volt [1eV = 1.602×10⁻¹⁹ J]
- Then:
 - momenta, energy, mass and temperature expressed in the same units [eV]
 - time and spatial coordinates expressed in the same units [1/ eV]



- the discovery of the neutron [Chadwick 1932] and thus that atomic nuclei are made of protons and neutrons, implies that:
 - a new force must exist to compensate the electric repulsion of protons and render atomic nuclei stable

must be strongly attractive



- must be very short range
 - Nutherford's early scattering experiments [low energy] of α-particles [He nuclei] on atomic nuclei could be explained by EM alone
 - > only at higher energies [when α-particles can approach the nuclei more closely] the effects of the strong force are felt
 - strong force only 'active' when nucleons 'touch' :: range of the order of nuclear diameter [10⁻¹⁵ m = 1 fm] :: timescale of the order 10⁻²³ s [10 ys]
 - must be independent of electric charge [act equally on protons and neutrons]

- in general heavier nuclei are more unstable [they decay]
 - supports picture of binding force having short range
 - ► if long range, the more nucleons the more stable
 - if just nearest neighbours than strong force on extra nucleon does not compensate electric repulsion amongst protons



- what is still missing from the discussion?
 - we want to describe strong interactions between elementary particles [which are not the protons and neutrons]

we will see later that the strong interaction can, in fact, be described [almost] analogously to the electromagnetic case

- the neutron decays spontaneously to a proton and an electron with a half-life [average time it takes for half of a sample to decay] of about 10 minutes
 - as this is much longer than the time-scales associated with the strong interaction [~10⁻²³ s] and it is difficult to conceive how EM interactions could contribute to this process
 - neutron decay must be due to some new force :: weak force
 - half-life of 10 min results from weakness of the interaction and small mass difference between neutron and proton

.

> the weak force underlies the radioactive β decay of nuclei



> the weak force underlies the radioactive β decay of nuclei



however, the electron [or positron] emerges with energy up to [but not always equal to the mass difference of the initial and final nuclei] :: apparent violation of energy conservation [also angular momentum]

Pauli [1930] postulated that a new invisible particle was also emitted in the decay and carried the missing energy [and angular momentum] :: the neutrino [named by Fermi]

Beta-minus Decay Nitrogen-14 Carbon-14 β Antineutrino Electron 6 protons 7 protons 8 neutrons 7 neutrons Beta-plus Decay Carbon-10 Boron-10 Neutrino Positron 6 protons 5 protons

the neutrino is uncharged [no EM interactions]

the neutrino 'invisibility' follows from the weakness of the weak interaction

THE PROGRAMME

- describe the [3] interactions experienced by the fundamental constituents of matter [elementary particles] in a unified theoretical framework
 - need to identify elementary particles
- theoretical description should/must:
 - respect relativistic invariance [as to make sense for speeds close to that of light]
 - respect quantum mechanics [as to make sense for small scales]
 - reflect fundamental symmetries
 - be consistent with experimental observations

A NOTE ON UNIFICATION

- distinguish two varieties of unification
 - physical unification :: understanding of distinct forces as manifestations of a common underlying interaction
 - electromagnetism = electricity + magnetism
 - [a further important example will come later]
 - formal :: description of distinct fundamental interactions within an unified theoretical formalism [common language fulfilling generic fundamental principles]
 - the focus of these lectures

THEORETICAL FRAMEWORK

- fundamental interactions [electromagetic, weak and strong OR as we will see later electro-weak and strong] are described by Renormalizable Relativistic Quantum Gauge Field theories
 - relativistic: the theories are Lorentz invariant
 - quantum: degrees of freedom are quantized
 - gauge: symmetry [we will get there]
 - field: the fundamental degrees of freedom are fields [objects that have a value – number, vector, higher tensor – in each space-time points]
 - renormalizable: no physical infinities

[PREVIEW] THE STANDARD MODEL





7

Z⁰

W⁺/W

Higgs Boson

Photon

g

Gluons



[PREVIEW] THE STANDARD MODEL





RELATIVISTIC INVARIANT QUANTUM MECHANICS

• The Schrodinger equation, which describes the time evolution of a wave function [a quantum system]

$$i\frac{\partial}{\partial t}\psi(\mathbf{x},t) = -\frac{1}{2m}\nabla^2\psi(\mathbf{x},t)$$

- is incompatible with special relativity
 - it relates energy momentum in the classical way ($E=p^2/m$)
 - it treats time and space differently

RELATIVISTIC INVARIANT QUANTUM MECHANICS

- relativistically we should have E²=p²+m² [recall c=1]
 - implies existence of 'negative energy' states

$$E = \pm \sqrt{\mathbf{p}^2 + m^2}$$

- to be [correctly] reinterpreted as anti-particles of positive energy
- insist that the correct equation is first order in time derivative [like the Schrodinger equation] and find Hamiltonian [operator on the rhs] that is local, linear in momentum [spatial derivatives] and gives the relativistic energy-momentum relation

RELATIVISTIC INVARIANT QUANTUM MECHANICS

- insist that the correct equation is first order in time derivative [like the Schrodinger equation] and find Hamiltonian [operator on the rhs] that is local, linear in momentum [spatial derivatives] and gives the relativistic energy-momentum relation [Dirac]
 - ➤ only works [you can try it out] if wave-futicationHist
 Component [which implies spin] and
 - Solution where α and β are four matrices that fulfill $\alpha \cdot \mathbf{p} + \beta m$

$$\alpha_i \alpha_j + \alpha_j \alpha_i = 2\delta_{ij}$$

$$\beta \alpha_i + \alpha_i \beta = 0 \qquad \qquad \beta^2 = 1$$

WHY FIELDS AS DEGREES OF FREEDOM?

- single-particle equations [like the Dirac equation] are limited in the sense that they do not allow for particle creation/destruction [they preserve particle number]
 - ➤ note that relativistic theories cannot have fixed particle number: relativistic effects are relevant for E ≥ mc² and at such energies particle production is possible [e.g., p+p → p+p+π⁰]
 - Lorentz invariance and variable particle number go hand-in-hand
- a multi-[and variable-] particle scenario is accommodated naturally in the concept of quantum field
 - think of a quantum field as an infinite collection of harmonic oscillators [a series of springs with masses attached]
 - when some of the oscillators become excited [they vibrate] at particular frequencies which correspond to excitations of the quantum field, that is to say to particles [field quanta]

WHY FIELDS AS DEGREES OF FREEDOM?

- the electron field is the [Fourier] sum of individual wavefunctions, with coefficients of each wavefunction representing the probability of creation/destruction of a quantum with a given wavelength (momentum)
 - ► this is what is often referred to as 2nd quantization

GAUGE SYMMETRY

- the conservation of electric charge implies [Noether's theorem] a global symmetry [a phase rotation for the fermion field]
- a gauge symmetry amounts to promoting the symmetry to local [realized for each and all spacetime locations]

$$\psi \to e^{i\alpha(x)}\psi$$

QUANTUM ELECTRODYNAMICS [QED]

FEYNMAN, TOMONAGA, SCHWINGER [1946–50 :: NOBEL 1965]

- describe interactions of charged fundamental particles [eg, electron]
- ingredients:
 - fermion fields [electron/positron are the quanta]
 - U(1) gauge symmetry : local charge conservation
 - theory [=Lagrangian] fully specified by requiring that only terms that respect gauge invariance and are renormalizable are allowed

QED :: BUILDING THE LAGRANGIAN

 start with kinetic term for fermion field [essentially the Lagrangian for which the Dirac equation is the Euler-Lagrange equation] :: [µ=0,1,2,3 :: all are 4-vectors]

 $\bar{\psi}(i\gamma^{\mu}\partial_{\mu}-m)\psi$

• which is invariant for the global symmetry [charge conservation]

 $\psi \to e^{i\alpha}\psi$

• but not for its gauge 'version'

$$\psi \to e^{i\alpha(x)}\psi : \bar{\psi}(\cdots)\psi \to \bar{\psi}\Big(i\gamma^{\mu}(\partial_{\mu}+i\partial_{\mu}\alpha(x))-m\Big)\psi$$

• invariance under the local [gauge] transformations can be restored by introducing a new [bosonic] field :: the photon :: that transforms as

$$A_{\mu}(x) \to A_{\mu}(x) + \frac{1}{e} \partial_{\mu} \alpha(x)$$

• then we build a covariant derivative

$$D_{\mu} = \partial_{\mu} - ieA_{\mu}(x)$$

• such that $\psi(i\gamma^\mu D_\mu-m)ar{\psi}$ is gauge invariant

QED :: BUILDING THE LAGRANGIAN

 once we introduced a new field, should check what new gauge invariant terms we can write. the only possibility is [a kinetic term for the photon]

$$-\frac{1}{4}F_{\mu\nu}F^{\mu\nu} \quad : \quad F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$$

then the full QED Lagrangian is given by

$$\mathcal{L}_{QED} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \psi (i\gamma^{\mu}D_{\mu} - m)\bar{\psi}$$
$$D_{\mu} = \partial_{\mu} - ieA_{\mu}(x)$$
$$e\psi\gamma^{\mu}A_{\mu}(x)\bar{\psi}$$

fermion-photon coupling [interaction]

fundamental interactions

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QED BUILDING BLOCKS :: FEYNMAN RULES

$$\alpha \longrightarrow \beta \longrightarrow \left(\frac{i}{\not p - m + i\varepsilon}\right)_{\beta\alpha}$$



β

$$\rightarrow \qquad \frac{-i\eta_{\mu\nu}}{p^2 + i\varepsilon}$$





- rules follow straightforwardly from Lagrangian
- any QED process can be 'assembled' from these building blocks

$$u = (k - p')^{*} = (p - k')^{*} \approx -2k \cdot p' \approx -2k' \cdot p$$

AN EXAMPLE :: [BHABBA SCATTERING]
$$\int_{q^{\mu}} u, \text{ and } \overline{u} \qquad e^{+}e^{-} \longrightarrow e^{+}e^{-}$$

$$u, \text{ and } \overline{v} \qquad e^{+}e^{-} \longrightarrow e^{+}e^{-}$$

$$v, \text{ and } \overline{v} \qquad e^{+}e^{-} \longrightarrow e^{+}e^{-}$$

$$u, \text{ and } \overline{v} \qquad e^{+}e^{-} \longrightarrow e^{+}e^{-}$$

$$u, \text{ and } \overline{v} \qquad e^{+}e^{-} \longrightarrow e^{+}e^{-}$$

$$u, \text{ and } \overline{v} \qquad v, \text{ and } \overline{v}$$

$$p^{\mu} \qquad p^{\mu}$$

$$u, \text{ and } \overline{v} \qquad v, \text{ and } \overline{v}$$

$$v, \text{ and } \overline{v} \qquad v, \text{ and } \overline{v}$$

$$v, \text{ and } \overline{v} \qquad v, \text{ and } \overline{v}$$

$$v, \text{ and } \overline{v}$$

$$u, \text{ and } \overline{v}$$

$$v, \text{ and } \overline{v}$$

 $\sqrt{\left((\bar{v}_k \gamma^\mu v_{k'}) (\bar{u}_{p'} \gamma_\mu u_p) \right)^*} \left((\bar{v}_k \gamma^\nu u_p) (\bar{u}_{p'} \gamma_\nu v_{k'}) \right)$

AN EXAMPLE :: [BHABBA SCATTERING]

► the cross section [what is observable] is obtained from the square $v_{v, and} \bar{v}_{v, and} \bar{v}_{v, and}$ of the total amplitude [the sum of the $v_{v, v_{(k-k)}^2} = 0$ is obtained from the square $v_{v, and} = 0$ for $v_{(k+k)}^2 = 0$

 $\gamma^{\mu} \longrightarrow e^{+} e^{\frac{\gamma^{\mu}}{v}} \xrightarrow{u, \text{ and } \bar{u}}$

 $\mathcal{M} = -e^{2} \left(\bar{v}_{k} \gamma^{\mu} v_{k'} \right) \frac{1}{(k-k')^{2}} \left(\bar{u}_{p'} \gamma_{\mu} u_{p} \right) + e^{2} \left(\bar{v}_{k} \gamma^{\nu} u_{p} \right) \frac{1}{(k+p)^{2}} \left(\bar{u}_{p'} \gamma_{\nu} v_{k'} \right)_{\mathcal{M}} = -e^{2} \left(\bar{v}_{k} \gamma^{\mu} v_{k'} \right) \frac{1}{(k-k')^{2}} \left(\bar{u}_{p'} \gamma_{\nu} v_{k'} \right)_{\mathcal{M}} + e^{2} \left(\bar{v}_{k} \gamma^{\nu} u_{p} \right) \frac{1}{(k+p)^{2}} \left(\bar{u}_{p'} \gamma_{\nu} v_{k'} \right)$ Averaged over spin
them] and summed over spins of final particles [because we do not distinguish] $= \frac{1}{4} \sum_{s=1}^{2} \sum_{j=1}^{2} \sum_{j=1}^{2} \sum_{j=1}^{2} \sum_{j=1}^{2} \sum_{j=1}^{2} |\mathcal{M}|^{2}$

 $|\mathcal{M}|^2$

$$\begin{aligned} \overline{|\mathcal{M}|^{2}} &= \frac{1}{(2s_{e-}+1)(2s_{e+}+1)} \sum_{\text{spins}} |\mathcal{M}|^{2} \quad \overline{(2s_{e-}} \quad |\mathcal{M}|^{2} = e^{4} \left| \frac{(\bar{v}_{k}\gamma^{\mu}v_{k'})(\bar{u}_{p'}\gamma_{\mu}u_{p})}{(k-k')^{2}} \right|^{2} \quad \text{(scattering)} \\ &= \frac{1}{4} \sum_{s=1}^{2} \sum_{s'=1}^{2} \sum_{r=1}^{2} \sum_{r'=1}^{2} |\mathcal{M}|^{2} \quad \frac{1}{4} \sum_{s=1}^{2} \quad -e^{4} \left(\frac{(\bar{v}_{k}\gamma^{\mu}v_{k'})(\bar{u}_{p'}\gamma_{\mu}u_{p})}{(k-k')^{2}} \right)^{*} \left(\frac{(\bar{v}_{k}\gamma^{\nu}u_{p})(\bar{u}_{p'}\gamma_{\nu}v_{k'})}{(k+p)^{2}} \right) \quad \text{(interference)} \\ &= \frac{1}{4} \sum_{s=1}^{2} \sum_{s'=1}^{2} \sum_{r=1}^{2} \sum_{r'=1}^{2} |\mathcal{M}|^{2} \quad \frac{1}{4} \sum_{s=1}^{2} \quad -e^{4} \left(\frac{(\bar{v}_{k}\gamma^{\mu}v_{k'})(\bar{u}_{p'}\gamma_{\mu}u_{p})}{(k-k')^{2}} \right) \left(\frac{(\bar{v}_{k}\gamma^{\nu}u_{p})(\bar{u}_{p'}\gamma_{\nu}v_{k'})}{(k+p)^{2}} \right)^{*} \quad \text{(interference)} \\ &= \frac{|\mathcal{M}|^{2}}{|\mathcal{M}|^{2}} \quad e^{4} \left| \frac{(\bar{v}_{k}}{k} + e^{4} \left| \frac{(\bar{v}_{k}\gamma^{\nu}u_{p})(\bar{u}_{p'}\gamma_{\nu}v_{k'})}{(k+p)^{2}} \right|^{2} \quad \text{(annihilation)} \end{aligned}$$

AN EXAMPLE :: [BHABBA SCATTERING]

• the result is very simple

$$egin{aligned} &\sum {u_p^{(s)} ar{u}_p^{(s)} = p\!\!\!/ + m} \ s = &(k+p)^2 = &(k'+p')^2 pprox & 2k \cdot p pprox & 2k' \cdot p' \ t = &(k-k')^2 = &(p-p')^2 pprox - 2k \cdot k' pprox - 2p \cdot p' \ u = &(k-p')^2 = &(p-k')^2 pprox - 2k \cdot p' pprox - 2k' \cdot p \end{aligned}$$

$$onumber p = \gamma^\mu p_\mu
onumber p_\mu
onumber q = \gamma^\mu \gamma^0$$



AN EXAMPLE :: [BHABBA SCATTERING]

► the result is very simple



THE LOOP CORRECTIONS :: RENORMALIZATION



- this type of correction leads to undistinguishable final states from the leading order diagrams [the initial and final states are the same]
- the momenta that 'run' in the loops is UNCONSTRAINED [it can be anything] and has to be integrated over as it is not an observable quantity
 - all these integrals lead to INFINITIES [which is not good]

THE LOOP CORRECTIONS :: RENORMALIZATION



- many methods to solve this infinity problem
 - In amount to reabsorbing the 'infinite' contributions into the constants in the Lagrangian [the mass, the coupling]
 - ➤ this is what is called renormalization
 - when it is possible to do it for a theory up to all orders [all loops] we say the theory is renormalizable
 - all physical theories must be renormalizable
THE RUNNING OF THE COUPLING

an immediate consequence of renormalization [of the vertex] is that the coupling 'constant' runs [changes] with energy :: the strength of the interaction changes with the energy/momentum [the inverse of the probing distance] of at which the interaction takes place



HOW WELL DOES QED WORK?

• the electron magnetic dipole moment is the magnetic moment of the electron due to its intrinsic properties [charge and spin]

- at leading order [if you wish from the Dirac equation] is g=2
 - loop-contributions give small corrections :: it has been calculated up to very high order [5th] in the coupling [which is a lot of work] and measured with matching precision

a= (g-2)/2

a[TH] = 0.001 159 652 181 643 (764)

a[EXP] = 0.001 159 652 180 73 (28)

 the theoretical prediction verified to highest accuracy in the history of Physics [and a very sensitive place to look for new physics (muon g-2) as with loops non-EM interactions also become relevant :: at present there is a mismatch of about 40 between theory and experiment]

STRONG INTERACTIONS :: FUNDAMENTAL PARTICLES

- over the 40-60s [of last century], as particle colliders became available, a large number of particles was discovered [many as resonances] experiencing the strong interaction
 - a seriously explored possibility was that ALL of them were fundamental [this went well with 60s political views]

AT A RECENT COUNT

1 Meson Summary Table

Baryon Summary	Tabl

See also the table of suggested $q\overline{q}$ quark-model assignments in the Quark Model section. Indicates particles that appear in the preceding Meson Summary Table. We do not regard the other entries as being established.

		STRANGE		CHARMED, STRANGE		$c\overline{c}$ continued			
	(S = C = C)	= B = 0)		$(S = \pm 1, C =$	= <i>B</i> = 0)	(C = S)	$=\pm1)$		$P(J^{PC})$
	Р(JFC)		$P(J^{rc})$		I(J ^r)	(+ possibly no	I P	 ψ₃(3842) 	0-(3)
• π^{\pm}	$1^{-}(0^{-})$	• \$\phi(1680)\$	$0^{-}(1^{-})$	• K [±]	1/2(0)	2 +	n(J)	χ _{c0} (3860)	0+(0++)
• π^0	$1^{-}(0^{-+})$	 ρ₃(1690) 	1+(3)	• K ⁰	1/2(0-)	• D_s^{\pm}	$0(0^{-})$	• χ _{c1} (3872)	$0^+(1^{++})$
• η	0+(0-+)	 ρ(1700) 	$1^{+}(1^{})$	• K_S^0	1/2(0)	• D_s^**	0(?')	• <i>Z_c</i> (3900)	$1^{+}(1^{+})$
• <i>f</i> ₀ (500)	$0^+(0^{++})$	• a ₂ (1700)	$1^{-}(2^{++})$	• K_L^0	1/2(0 ⁻)	• $D_{s0}^*(2317)^{\pm}$	0(0+)	• X(3915)	$0^+(0/2^{++})$
 ρ(770) 	$1^+(1^{})$	• f ₀ (1710)	$0^+(0^{++})$	• K ₀ (700)	1/2(0+)	• $D_{s1}(2460)^{\pm}$	0(1+)	• χ _{c2} (3930)	$0^+(2^++)$
• ω(782)	$0^{-}(1^{-})$	η (1760)	0+(0 - +)	• K*(892)	$1/2(1^{-})$	• D _{\$1} (2536) [±]	0(1+)	X(3940)	?'(?'')
• η′(958)	0+(0-+)	• <i>π</i> (1800)	$1^{-}(0^{-+})$	• K ₁ (1270)	$1/2(1^+)$	• $D_{s2}^*(2573)$	0(2+)	• X(4020) [±]	$1^+(?^{!-})$
• f ₀ (980)	$0^+(0^{++})$	$f_2(1810)$	$0^+(2^{++})$	• K ₁ (1400)	$1/2(1^+)$	• $D_{s1}^*(2700)^{\pm}$	0(1-)	• \u03c9 (4040)	$0^{-}(1^{-})$
• <i>a</i> ₀ (980)	$1^{-}(0^{++})$	X(1835)	?!(0 - +)	• K*(1410)	$1/2(1^{-})$	$D_{s1}^{*}(2860)^{\pm}$	0(1-)	$X(4050)^{\pm}$	$1^{-}(?^{+})$
 φ(1020) 	$0^{-}(1^{-})$	• φ ₃ (1850)	0-(3)	• K ₀ (1430)	1/2(0+)	$D_{s3}^{*}(2860)^{\pm}$	0(3-)	$X(4055)^{\pm}$	$1^{+}(?^{*})$
• $h_1(1170)$	$0^{-}(1^{+})$	• η ₂ (1870)	$0^+(2^{-+})$	• K ₂ (1430)	$1/2(2^+)$	X ₀ (2900)	?(0+)	$X(4100)^{\pm}$	$1 (? \cdot \cdot)$
• b ₁ (1235)	$1^+(1^+)$	• π ₂ (1880)	$1^{-}(2^{-+})$	• K(1460)	1/2(0)	$X_1(2900)$	$?(1^{-})$	• $\chi_{c1}(4140)$	$0 \cdot (1 + 1)$
• $a_1(1260)$	1(1 + 1)	$\rho(1900)$	$1^{+}(1^{})$	$K_2(1580)$	$1/2(2^{-})$	$D_{sJ}(3040)^{\pm}$	* 0(? [?])	• ψ(4160)	0(1)
• t ₂ (1270)	$0^{+}(2^{++})$	$f_2(1910)$	$0^+(2^++)$	K(1630)	1/2(?')	POT	OM	X (4160)	((?))
• <i>T</i> ₁ (1285)	$0^{+}(1^{+})$	$a_0(1950)$	1 (0 + 1)	• $K_1(1650)$	$1/2(1^+)$	(B =	+1)	$Z_{c}(4200)$	$1 \cdot (1)$
• η(1295) (1200)	$0^{+}(0^{-+})$	• $T_2(1950)$	$0^{+}(2^{++})$	• K*(1680)	1/2(1-)	(- . D ⁺	1/2(0-)	• $\psi(4230)$	0(1)
• $\pi(1300)$	1 (0 +) 1 - (2 + +)	• $a_4(1970)$	1 (4 +) 1 + (2)	• $K_2(1770)$	1/2(2-)	• <i>D</i> ⁻	1/2(0)	$K_{c0}(4240)$	$1^{-}(0^{+})$
• $a_2(1320)$	1(2++)	$\rho_3(1990)$	$\frac{1}{(3)}$	• K ₃ (1780)	1/2(3)			ス(4250) ⁻	1 (! - 1)
$\bullet I_0(1370)$	$0^{-}(0^{-})$ $1^{-}(1^{-}+)$	$\pi_2(2005)$	1(2')	• K ₂ (1820)	1/2(2-)	• $D^{-}/D^{-}AD$	/h honion	$\psi(4200)$	0(1)
• $\pi_1(1400)$	1(1 +)	• $I_2(2010)$	$0^{+}(2^{+})$	K(1830)	1/2(0-)		? <i>D</i> =DaryOn RF	• $\chi_{C1}(4274)$	$0^{+}(2^{2}+)$
• $\eta(1405)$	$0^{-}(0^{+})$	$I_0(2020)$	$0^+(0^{++})$	$K_0^*(1950)$	$1/2(0^+)$	V_{cb} and V_{ub}	CKM Ma-	A (4350)	$0^{-}(1^{-})$
• $h_1(1413)$ • $f_1(1420)$	$0^{+}(1^{+})$	\bullet $74(2050)$	$1^{-}(2^{-}+)$	• K ₂ (1980)	$1/2(2^+)$	trix Element	ts	$\psi(4300)$	$0^{-}(1^{-})$
• (1420)	$0^{-}(1^{-})$	$f_{2}(2100)$	$0^{+}(0^{+}^{+})$	• K ₄ (2045)	1/2(4+)	• B*	1/2(1)	• $\psi(4415)$	$0^{-}(1^{-})$
$f_{6}(1430)$	$0^{+}(2^{+})$	$f_0(2100)$ $f_2(2150)$	$0^{+}(2^{+}+)$	$K_2(2250)$	1/2(2-)	• $B_1(5/21)$ $P_2(5722)$	$\frac{1}{2(1^{\circ})}$	• Z _c (4430)	$1^{+}(1^{+}-)$
• $a_0(1450)$	$1^{-}(0^{++})$	a(2150)	$1^{+}(1^{-})$	$K_3(2320)$	1/2(3+)	$D_{j}(5752)$	$\frac{1}{2}(2^{+})$	$\chi_{c0}(4500)$	$0^{+}(0^{+}+)$
				1/2/00000	- (O/E -)				/
 ρ(1450) 	$1^{+}(1^{-})$	 φ(2130) φ(2170) 	$0^{-}(1^{-})$	K ₅ (2380)	$1/2(5^{-})$	$\bullet D_2(5747)$ B (5840)	$\frac{1}{2(2^{+})}$ $\frac{1}{2(2^{?})}$	 ψ(4660) 	$0^{-}(1^{-})$
 ρ(1450) η(1475) 	$1^+(1^-)^{\prime}$ $0^+(0^-)^{\prime}$	• $\phi(2170)$ $f_0(2200)$	$0^{-}(1^{-})^{-}$ $0^{+}(0^{+})^{+}$	$K_5(2380)$ $K_4(2500)$	$1/2(5^{-})$ $1/2(4^{-})$	• $B_2(5747)$ $B_3(5840)$ • $B_4(5970)$	$1/2(2^{\circ})$ $1/2(?^{\circ})$ $1/2(?^{\circ})$	• $\psi(4660)$ $\chi_{c0}(4700)$	$0^{-}(1^{-}))$ $0^{+}(0^{+})$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$	$1^{+}(1^{-})^{-}$ $0^{+}(0^{-})^{+}$ $0^{+}(0^{+})^{-}$	• $\phi(2170)$ • $f_0(2200)$ • $f_J(2220)$	$0^{-}(1^{-}))$ $0^{+}(0^{+}+))$ $0^{+}(2^{+}+)$	K ₅ (2380) K ₄ (2500) K(3100)	$1/2(5^{-})$ $1/2(4^{-})$? [?] (? ^{??})	• B ₂ (5747) B _J (5840) • B _J (5970)	$1/2(?^{?})$ $1/2(?^{?})$ $1/2(?^{?})$	• $\psi(4660)$ $\chi_{c0}(4700)$	$0^{-(1)}_{0^{+}(0^{+}+)}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ $f_1(1510)$	$\begin{array}{c} 1^{+}(1^{-}-) \\ 0^{+}(0^{-}+) \\ 0^{+}(0^{+}+) \\ 0^{+}(1^{+}+) \end{array}$	• $\phi(2170)$ • $f_0(2200)$ $f_J(2220)$	$0^{-}(1^{-})$ $0^{+}(0^{+}+)$ $0^{+}(2^{+}+)$ or $4^{+}+)$	K ₅ (2380) K ₄ (2500) K(3100) CHARM	1/2(5 ⁻) 1/2(4 ⁻) ? [?] (? ^{??}) IED	• B ₂ (5747) B _J (5840) • B _J (5970) BOTTOM, 2	1/2(? [?]) 1/2(? [?]) STRANGE	• $\psi(4660)$ $\chi_{c0}(4700)$	$\frac{0^{-}(1^{-})}{0^{+}(0^{+})}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ $f_1(1510)$ • $f'_2(1525)$	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ \end{array}$	• $\phi(2170)$ • $f_0(2200)$ $f_J(2220)$ $\eta(2225)$	$\begin{array}{c} 0^{-}(1) \\ 0^{+}(0 + +) \\ 0^{+}(2 + +) \\ 0^{+}(2 + +) \\ 0^{+}(0 - +) \end{array}$	$K_5^*(2380)$ $K_4(2500)$ K(3100) CHARM $(C = \pm$	1/2(5 ⁻) 1/2(4 ⁻) ? [?] (? ^{??}) MED	• $B_2(5747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, 2 $(B = \pm 1, -1)$	$1/2(2^+)$ $1/2(?^2)$ $1/2(?^2)$ STRANGE $S = \mp 1$	• $\psi(4660)$ $\chi_{c0}(4700)$ (+ possibly no	$\frac{0^{-}(1^{-})}{0^{+}(0^{+})}$ $\frac{\overline{b}}{\overline{b}}$ $\frac{1}{\overline{b}}$ $\frac{1}{$
$\begin{array}{c} \rho(1450) \\ \bullet \ \rho(1450) \\ \bullet \ \eta(1475) \\ \bullet \ f_0(1500) \\ f_1(1510) \\ \bullet \ f'_2(1525) \\ f_2(1565) \end{array}$		$ \begin{aligned} & \phi(2170) \\ & f_0(2200) \\ & f_J(2220) \\ & \eta(2225) \\ & \rho_3(2250) \end{aligned} $	$\begin{array}{c} 0^{-}(1) \\ 0^{+}(0^{+}+) \\ 0^{+}(2^{+}+) \\ 0^{+}(0^{-}+) \\ 1^{+}(3^{-}-) \end{array}$	$K_5^*(2380)$ $K_4(2500)$ K(3100) CHARM $(C = \pm$ • D^{\pm}	1/2(5 ⁻) 1/2(4 ⁻) ? [?] (? ^{??}) MED :1) 1/2(0 ⁻)	• $B_2(5747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, 1 ($B = \pm 1$, • B_s^0	$\frac{1/2(2^{+})}{1/2(?^{+})}$ $\frac{1/2(?^{+})}{1/2(?^{+})}$ STRANGE $S = \mp 1$ $0(0^{-})$	• $\psi(4660)$ $\chi_{c0}(4700)$ (+ possibly no • $\eta_b(1S)$	$0^{-}(1^{-})^{-}(0^{+})^{-}(0^{+})^{-}(0^{+})^{-}$ $\overline{b}^{-}(0^{+})^{-}(0^{-})^{-}(0^$
$ \begin{array}{c} \circ \rho(1450) \\ \bullet \rho(1450) \\ \bullet \eta(1475) \\ \bullet f_0(1500) \\ f_1(1510) \\ \bullet f'_2(1525) \\ f_2(1565) \\ \rho(1570) \end{array} $	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ \end{array}$	• $\phi(2170)$ $f_0(2200)$ $f_1(2220)$ $\eta(2225)$ $\rho_3(2250)$ • $f_2(2300)$	$\begin{array}{c} 0^{-}(1) \\ 0^{+}(0++) \\ 0^{+}(2++) \\ 0^{+}(2++) \\ 0^{+}(0-+) \\ 1^{+}(3) \\ 0^{+}(2++) \\ 0^{+}(2++) \end{array}$	$K_5^*(2380)$ $K_4(2500)$ K(3100) CHARM $(C = \pm$ D^{\pm} D^0	$\frac{1/2(5^{-})}{1/2(4^{-})}$??(???) $\frac{1}{1/2(0^{-})}$ $\frac{1/2(0^{-})}{1/2(0^{-})}$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, 1° ($B = \pm 1$, • B_S° • B_S°	$\frac{1/2(2^{+})}{1/2(?^{+})}$ $\frac{1/2(?^{+})}{1/2(?^{+})}$ STRANGE $\frac{5}{5} = \mp 1$ $0(0^{-})$ $0(1^{-})$	• $\psi(4660)$ $\chi_{c0}(4700)$ (+ possibly no • $\eta_b(1S)$ • $\Upsilon(1S)$	$\frac{0^{-}(1^{-})}{0^{+}(0^{+})}$ $\frac{\overline{b}}{\overline{b}}$ $\frac{0^{+}(0^{-})}{0^{-}(1^{-})}$ $\frac{0^{+}(0^{+})}{0^{+}(0^{+}+1)}$
$ \begin{array}{c} \circ \rho(1450) \\ \circ \rho(1450) \\ \bullet \eta(1475) \\ \bullet f_0(1500) \\ f_1(1510) \\ \bullet f'_2(1525) \\ f_2(1565) \\ \rho(1570) \\ h_1(1595) \end{array} $	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 0-(1+-)\\ \end{array}$	• $\phi(2170)$ $f_0(2200)$ $f_1(2220)$ $\eta(2225)$ $\rho_3(2250)$ • $f_2(2300)$ $f_4(2300)$	$\begin{array}{c} 0^{-}(1)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0-+)\\ 1^{+}(3)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(4++)\\$	$K_{5}^{*}(2380)$ $K_{4}(2500)$ $K(3100)$ CHARM (C = ± • D [±] • D ⁰ • D*(2007) ⁰	$\frac{1/2(5^{-})}{1/2(4^{-})}$ $\frac{1/2(4^{-})}{?^{?}(?^{??})}$ $\frac{1}{1/2(0^{-})}$ $\frac{1/2(0^{-})}{1/2(1^{-})}$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, 2 ($B = \pm 1$, • B_s^0 • B_s^* $X(5568)^{\pm}$	$\frac{1/2(2^{+})}{1/2(?^{2})}$ $\frac{1}{2(?^{2})}$ STRANGE $\frac{5}{5} = \mp 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$	• $\psi(4660)$ $\chi_{c0}(4700)$ • $\psi(4660)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$	$\frac{0^{-}(1^{-})}{0^{+}(0^{+})}$ $\frac{\overline{b}}{\overline{b}}$ $\frac{\overline{b}}{0^{+}(0^{-}+)}$ $\frac{0^{+}(0^{-}+)}{0^{-}(1^{-}-)}$ $\frac{0^{+}(0^{+}+)}{0^{+}(0^{+}+)}$
$ \begin{array}{l} \bullet \rho(1450) \\ \bullet \eta(1475) \\ \bullet f_0(1500) \\ f_1(1510) \\ \bullet f'_2(1525) \\ f_2(1565) \\ \rho(1570) \\ h_1(1595) \\ \bullet \pi_1(1600) \end{array} $	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1-+)\\ 1-(1-+)\\ \end{array}$	• $\phi(2170)$ $f_0(2200)$ $f_1(2220)$ $\eta(2225)$ $\rho_3(2250)$ • $f_2(2300)$ $f_4(2300)$ $f_6(2300)$	$\begin{array}{c} 0^{-}(1)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ \mathbf{a}^{+}(0-+)\\ 1^{+}(3)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(4++)\\ 0^{+}(0+$	$K_{5}^{*}(2380)$ $K_{4}(2500)$ $K(3100)$ CHARM (C = ± • D [±] • D ⁰ • D [*] (2007) ⁰ • D [*] (2010) [±]	1/2(5 ⁻) 1/2(4 ⁻) ? [?] (? [?]) IED 1/2(0 ⁻) 1/2(0 ⁻) 1/2(1 ⁻) 1/2(1 ⁻)	• $B_2(3147)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, 1 ($B = \pm 1$, • B_5^0 • B_5^* × $X(5568)^{\pm}$ • $B_{51}(5830)^0$	$\frac{1/2(2^{-})}{1/2(?^{2})}$ $\frac{1/2(?^{2})}{1/2(?^{2})}$ STRANGE $S = \mp 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$	• $\psi(4600)$ $\chi_{c0}(4700)$ • $\psi(4600)$ (+ possibly no • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $\chi_{b1}(1P)$	$\begin{array}{c} 0^{-}(1^{-}) \\ 0^{+}(0^{+}) \\ \hline b \\ \overline{b} \\ 0^{-}(q\overline{q} \text{ states}) \\ 0^{+}(0^{-}) \\ 0^{-}(1^{-}) \\ 0^{+}(0^{+}) \\ 0^{+}(1^{+}) \\ 0^{-}(1^{+}) \\ 0^{-}(1^{+}) \end{array}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f'_2(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 1-(1++)\\ 0+(2++)\\ 0+(2++)\\ 1-(1++)\\ 0+(2+$	$ \begin{array}{l} \bullet \phi(2170) \\ f_0(2200) \\ f_J(2220) \\ \hline \\ \phi_3(2250) \\ \bullet f_2(2300) \\ f_4(2300) \\ f_0(2330) \\ \bullet f_2(2340) \\ \bullet f_2(2340) \\ \hline \\ \bullet f_2(2340) \\ \bullet f_2(2340) \\ \hline \end{array} $	$\begin{array}{c} 0^{-}(1-) \\ 0^{+}(0++) \\ 0^{+}(2++) \\ 0^{+}(0-+) \\ 1^{+}(3) \\ 0^{+}(2++) \\ 0^{+}(2++) \\ 0^{+}(4++) \\ 0^{+}(0++) \\ 0^{+}(0++) \\ 0^{+}(2+-) \\ 1^{+}(2-+) \\ 0^{+}(2++) \\$	$\begin{array}{c} \kappa_{5}^{*}(2380) \\ \kappa_{4}(2500) \\ \kappa(3100) \\ \end{array}$ $\begin{array}{c} CHARM \\ (C = \pm \\ \bullet D^{\pm} \\ \bullet D^{0} \\ \bullet D^{*}(2007)^{0} \\ \bullet D^{*}(2010)^{\pm} \\ \bullet D_{0}^{*}(2300) \end{array}$	1/2(5 ⁻) 1/2(4 ⁻) ? [?] (? [?]) 1ED 1/2(0 ⁻) 1/2(0 ⁻) 1/2(1 ⁻) 1/2(1 ⁻) 1/2(1 ⁻) 1/2(0 ⁺)	• $B_2(5147)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, 1 ($B = \pm 1$, • B_5^0 • B_5^* $X(5568)^{\pm}$ • $B_{51}(5830)^0$ • $B_{52}^*(5840)^0$	$\frac{1/2(2^{-})}{1/2(?^{2})}$ $\frac{1/2(?^{2})}{1/2(?^{2})}$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$	• $\psi(4660)$ $\chi_{c0}(4700)$ • $\psi(4660)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $\chi_{b1}(1P)$ • $\chi_{b1}(1P)$	$\frac{0}{0} - (1) \\ 0 + (0 + +) \\ 0 - q\bar{q} \text{ states}) \\ 0 + (0 - +) \\ 0 - (1) \\ 0 + (0 + +) \\ 0 - (1 + -) \\ 0 - (1 + -) \\ 0 + (2 + +) $
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f'_2(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 1-(1++)\\ 0+(2+$	$\begin{array}{l} \bullet \phi(2170) \\ f_0(2200) \\ f_1(2220) \\ \hline \\ \phi_3(2250) \\ \bullet f_2(2300) \\ f_4(2300) \\ f_0(2330) \\ \bullet f_2(2340) \\ \phi_5(2350) \\ \phi_5(2350) \\ \hline \end{array}$	$\begin{array}{c} 0^{-}(1)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0-+)\\ 1^{+}(3)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 1^{+}(5)\\ 2^{2}(2^{2})\\ 2^{2}\end{array}$	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ \bullet D^0 \\ \bullet D^*(2007)^0 \\ \bullet D^*(2010)^\pm \\ \bullet D_0^*(2300) \\ \bullet D_1(2420) \\ \hline \end{array}$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(5147)$ $B_J(5840)$ • $B_J(5970)$ BOTTOM, $E_3(B_2 \pm 1, 0)$ • $B_5^{\rm c}$ • $B_5^{\rm c}$ • $B_{5}^{\rm c}$ • $B_{51}(5830)^0$ • $B_{52}^{\rm c}(5840)^0$ $B_{sJ}^{\rm c}(5850)$	$\frac{1/2(2^{-})}{1/2(?^{2})}$ $\frac{1/2(?^{2})}{1/2(?^{2})}$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$ $?(?^{2})$	• $\psi(4660)$ $\chi_{c0}(4700)$ • $\psi(4660)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $h_b(1P)$ • $\chi_{b2}(1P)$ • $\chi_{b2}(1P)$	$\frac{0}{0} - (1) \\ 0 + (0 + +) \\ 0 - q\bar{q} \text{ states}) \\ 0^{+} (0 - +) \\ 0^{-} (1) \\ 0^{+} (0 + +) \\ 0^{+} (1 + +) \\ 0^{-} (1 + -) \\ 0^{+} (2 + +) \\ 0^{+} (2 - +) \\ 0^{+} (0 - +) \\ 0^$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f'_2(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1645)$	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 0+(2++)\\ 0+(2-+)\\ 0+(2-+)\\ 0-(1)\\ 0-(1)\\ 0+(2-+)\\ 0+(2-$	$\begin{array}{l} \bullet \phi(2170) \\ f_0(2220) \\ f_1(2220) \\ \hline \\ \phi_3(2250) \\ \bullet f_2(2300) \\ f_2(2300) \\ f_4(2300) \\ f_0(2330) \\ \bullet f_2(2340) \\ \rho_5(2350) \\ \chi(2370) \\ \chi$	$\begin{array}{c} 0^{-}(1-)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0-+)\\ 1^{+}(3)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0++)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 1^{+}(5)\\ ?^{2}(?)\\ ?^{2}(?)\\ 2^{+}(2++)\\ 2^{+$	$\begin{array}{c} \kappa_5^*(2380) \\ \kappa_4(2500) \\ \kappa(3100) \\ \hline \\ \hline \\ CHARM \\ (C = \pm \\ 0 \\ D^{\pm} \\ D^0 \\ D^*(2007)^0 \\ D^*(2010)^{\pm} \\ D^*_0(2300) \\ D_1(2420) \\ D_1(2430)^0 \\ \end{array}$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(5147)$ $B_J(5840)$ • $B_J(5970)$ BOTTOM, $E_3(B = \pm 1, B_5)$ • $B_5^{\rm c}$ • $B_5^{\rm c}$ • $B_{51}(5830)^0$ • $B_{52}^{\rm c}(5840)^0$ $B_{5J}^{\rm c}(5850)$	$\frac{1}{2(2^{-})}$ $\frac{1}{2(?^{2})}$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$ $?(?^{2})$ CHARMED	• $\psi(4660)$ $\chi_{c0}(4700)$ • $\psi(4660)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $\lambda_{b1}(1P)$ • $h_b(1P)$ • $\chi_{b2}(1P)$ $\eta_b(2S)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array}$ $\overline{b} \\ \overline{b} \\ 0 - q \overline{q} \text{ states}) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^+ (1 + -) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^+ (0 - +) \\ 0^- (1) \end{array}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f_2'(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1645)$ • $\omega(1650)$	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 1-(1++)\\ 0+(2++)\\ 0+(2-+)\\ 0-(1)\\ 0-(2-$	$\begin{array}{l} \bullet \phi(2170) \\ f_0(2220) \\ f_J(2220) \\ \hline \\ \rho_3(2250) \\ \bullet f_2(2300) \\ f_4(2300) \\ f_0(2330) \\ \bullet f_2(2340) \\ \rho_5(2350) \\ \chi(2370) \\ f_6(2510) \end{array}$	$\begin{array}{c} 0^{-}(1)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0-+)\\ 1^{+}(3)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 1^{+}(5)\\ ?^{2}(?^{2})\\ 0^{+}(6++)\\ \end{array}$	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0 \\ D^{\pm} \\ 0 \\ D^{\pm} (2007)^{0} \\ D^{\pm} (2010)^{\pm} \\ D_0^*(2010)^{\pm} \\ D_0^*(2300) \\ D_1(2420) \\ D_1(2430)^{0} \\ D_2^*(2460) \\ D_2^*(2460) \\ D_0 \\ D_0^*(200) \\ D$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(5147)$ $B_J(5840)$ • $B_J(5970)$ BOTTOM, $E_{(B=\pm 1, 1)}$ • B_5^0 • B_5^* × $X(5568)^{\pm}$ • $B_{51}(5830)^0$ • $B_{52}^*(5840)^0$ $B_{5J}^*(5850)$ BOTTOM, $G_{(B=C)}$	$\frac{1}{2(2^{-})}$ $\frac{1}{2(?^{2})}$ $\frac{1}{2(?^{2})}$ STRANGE $\frac{5}{5} = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$ $?(?^{2})$ CHARMED $= \pm 1$	• $\psi(4660)$ $\chi_{c0}(4700)$ • $\psi(4660)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $\lambda_{b1}(1P)$ • $\lambda_{b2}(1P)$ • $\eta_b(2S)$ • $\gamma(2S)$ • $\gamma(2S)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array}$ $\overline{b} \\ \overline{b} \\ 0 - q \overline{q} \text{ states}) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^+ (2 + +) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^- (2) \end{array}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f'_2(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$ • $\eta_2(1645)$ • $\omega(1650)$ • $\omega_3(1670)$	$\begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2-+)\\ 0-(1)\\ 0-(3)\\ 1-(2-+)\\ \end{array}$	 φ(2170) f₀(2200) f₁(2220) f₂(2220) f₂(2250) f₂(2300) f₂(2300) f₀(2330) f₂(2340) ρ₅(2350) X(2370) f₆(2510) OTHEF 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(4++) 0+(0++) 0+(0++) 0+(2++) 1+(5) ?'(?') 0+(6++) CLIGHT	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0.000 $	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(5147)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 \pm 1, 0)$ • B_5° • B_5° • $B_{51}^{\circ}(5850)^{\pm}$ • $B_{52}^{\circ}(5840)^{0}$ $B_{52}^{\circ}(5840)^{0}$ BOTTOM, $C_{(B=C)}^{\circ}$	$\frac{1}{2(2^{-})}$ $\frac{1}{2(?^{2})}$ $\frac{1}{2(?^{2})}$ STRANGE $\frac{5}{5} = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$ $?(?^{2})$ CHARMED $= \pm 1$ $0(0^{-})$	• $\psi(4660)$ $\chi_{c0}(4700)$ • $\psi(4660)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $h_b(1P)$ • $\chi_{b2}(1P)$ • $\eta_b(2S)$ • $\gamma(2S)$ • $\gamma(2F)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array}$ $\overline{b} \\ \overline{b} \\ 0 - q \overline{q} \text{ states}) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^- (2) \\ 0^+ (0 + +) \end{array}$
$\begin{array}{l} \circ\rho(1450)\\ \circ\eta(1475)\\ \circf_0(1500)\\ f_1(1510)\\ \circf_2'(1525)\\ f_2(1565)\\ \rho(1570)\\ h_1(1595)\\ \circ\pi_1(1600)\\ \circa_1(1640)\\ f_2'(1640)\\ \circ\eta_2(1645)\\ \circ\omega_1(1670)\\ \circ\pi_2(1670)\\ \circ\pi_2(1670)\\ \end{array}$		• φ(2170) f ₀ (2200) f ₁ (2220) • f ₂ (2220) • f ₂ (2250) • f ₂ (2300) f ₀ (2330) • f ₂ (2340) ρ ₅ (2350) X(2370) f ₆ (2510) OTHEF Further St	$\begin{array}{c} 0^{-}(1)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0-+)\\ 1^{+}(3)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(6++)\\ 0^{+}(6++)\\ \hline \end{array}$	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0.000 \\ D^{\pm} \\ 0.000 \\ D^{\pm} (2007)^0 \\ D^{\pm} (2010)^{\pm} \\ D_0^*(2010)^{\pm} \\ D_0^*(2010)^{\pm} \\ D_0^*(2010)^{\pm} \\ D_1(2420) \\ D_1(2420$	$\frac{1/2(5^{-})}{1/2(4^{-})}, \frac{1}{2^{2}(7^{2})}$ $\frac{1}{1/2(0^{-})}, \frac{1}{1/2(0^{-})}, \frac{1}{1/2(1^{-})}, \frac{1}{1/2(1^{-})}, \frac{1}{1/2(1^{+})}, \frac{1}{1/2(2^{+})}, \frac{1}{1/2(2^{+})}, \frac{1}{1/2(0^{-})}, \frac{1}{1/2(0^{-})}, \frac{1}{1/2(1^{-})}, \frac{1}{1/2(2^{-})}, \frac{1}{1/2(2^{-})}$	• $B_2(5147)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 \pm 1, 0)$ • B_5° • B_5° • B_5° • $B_{51}(5830)^{0}$ • $B_{52}^{\circ}(5840)^{0}$ $B_{52}^{\circ}(5840)^{0}$ BOTTOM, $C_{(B=C)}^{\circ}$ • B_c^{+} • B_c^{-} • B_c^{+}	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $2(2^{+})$ $0(2^{+})$ $2(2^{+$	• $\psi(4600)$ $\chi_{c0}(4700)$ • $\psi(4600)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $h_b(1P)$ • $\lambda_{b2}(1P)$ $\eta_b(2S)$ • $\gamma(2S)$ • $\gamma_{2}(1D)$ • $\chi_{b0}(2P)$ • $\chi_{b0}(2P)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array}$ $\overline{b} \\ \overline{b} \\ 0 - q \overline{q} \text{ states}) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^- (2) \\ 0^- (2) \\ 0^+ (0 + +) \\ 0^+ (1 + +) \end{array}$
$ \begin{array}{l} \circ \rho(1450) \\ \circ \eta(1475) \\ \circ f_0(1500) \\ f_1(1510) \\ \circ f'_2(1525) \\ f_2(1565) \\ \rho(1570) \\ h_1(1595) \\ \circ \pi_1(1600) \\ \circ a_1(1640) \\ f'_2(1640) \\ \circ \eta_2(1645) \\ \circ \omega_1(1670) \\ \circ \pi_2(1670) \\ \end{array} $		$\begin{array}{l} \bullet \phi(2170) \\ f_0(2220) \\ f_J(2220) \\ \phi_3(2250) \\ \bullet f_2(2300) \\ f_2(2300) \\ f_4(2300) \\ f_0(2330) \\ \bullet f_2(2340) \\ \rho_5(2350) \\ \chi(2370) \\ f_6(2510) \\ \hline \\ $	$\begin{array}{c} 0^{-}(1)\\ 0^{+}(0++)\\ 0^{+}(2++)\\ 0^{+}(2++)\\ 0^{+}(0-+)\\ 1^{+}(3)\\ 0^{+}(2++)\\$	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0.5 \\ 0.$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(3147)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 \pm 1, 0)$ • B_5^8 • B_5^8 • $X(5568)^{\pm}$ • $B_{51}(5830)^0$ • $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ BOTTOM, $C_{(B=C)}^{*}$ • B_c^+ • $B_c(2S)^{\pm}$	$\frac{1}{2(2^{-})}$ $\frac{1}{2(?^{2})}$ $\frac{1}$	• $\psi(460)$ $\chi_{c0}(4700)$ • $\psi(460)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $h_b(1P)$ • $\chi_{b2}(1P)$ $\eta_b(2S)$ • $\gamma(2S)$ • $\gamma(2S)$ • $\gamma(2S)$ • $\chi_{b0}(2P)$ • $\chi_{b1}(2P)$ • $h_b(2P)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array}$ $\overline{b} \\ \overline{b} \\ 0 - q \overline{q} \text{ states}) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^- (2) \\ 0^- (2) \\ 0^- (0 + +) \\ 0^- (1 + -) \\ 0^- (1 + -) \\ 0^- (1 + -) \end{array}$
$ \begin{array}{l} \circ \rho(1450) \\ \circ \eta(1475) \\ \circ f_0(1500) \\ f_1(1510) \\ \circ f'_2(1525) \\ f_2(1565) \\ \rho(1570) \\ h_1(1595) \\ \circ \pi_1(1600) \\ \circ a_1(1640) \\ f'_2(1640) \\ \circ \eta_2(1645) \\ \circ \omega_1(1670) \\ \circ \pi_2(1670) \\ \end{array} $		• $\phi(2170)$ $f_0(2220)$ $f_J(2220)$ $f_J(2220)$ • $f_2(2220)$ • $f_2(2250)$ • $f_2(2300)$ $f_4(2300)$ $f_0(2330)$ • $f_2(2340)$ $\rho_5(2350)$ X(2370) $f_6(2510)$ OTHEFF Further St.	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0.5 \\ 0.$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $B_2(5970)$ • $B_3^{\rm c}$ • $B_5^{\rm c}$ • $B_5^{\rm c}$ • $B_{51}(5830)^0$ • $B_{52}^{\rm c}(5840)^0$ $B_{52}^{\rm c}(5840)^0$ BOTTOM, $C_{(B=C)}^{\rm c}$ • $B_c^{\rm c}$ • $B_c^{\rm c}$	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $\frac{5}{5} = \pm 1$ $0(0^{-})$ $0(1^{-})$ $2(2^{+})$ $0(1^{+})$ $0(2^{+})$ $2(2^{+})$ $2(2^{+})$ $2(2^{+})$ $2(2^{+})$ $2(2^{-})$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$	• $\psi(460)$ $\chi_{c0}(4700)$ • $\psi(460)$ $\chi_{c0}(4700)$ • $\eta_b(1S)$ • $\gamma(1S)$ • $\chi_{b0}(1P)$ • $\chi_{b1}(1P)$ • $h_b(1P)$ • $\chi_{b2}(1P)$ $\eta_b(2S)$ • $\gamma(2S)$ • $\gamma(2S)$ • $\gamma(2S)$ • $\chi_{b0}(2P)$ • $\chi_{b1}(2P)$ • $h_b(2P)$ • $\chi_{b2}(2P)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array}$ $\overline{b} \\ \overline{b} \\ 0 - q \overline{q} \text{ states}) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^- (2) \\ 0^- (2) \\ 0^- (0 + +) \\ 0^- (1 + -) \\ 0^+ (1 + +) \\ 0^- (1 + -) \\ 0^- (1 + -) \\ 0^- (1 + -) \\ 0^+ (2 + +) \\ 0^- (1 + -) \\ 0^+ (2 + +) \end{array}$
$ \begin{array}{l} \circ \rho(1450) \\ \circ \eta(1475) \\ \circ f_0(1500) \\ f_1(1510) \\ \circ f'_2(1525) \\ f_2(1565) \\ \rho(1570) \\ h_1(1595) \\ \circ \pi_1(1600) \\ \circ a_1(1640) \\ f'_2(1640) \\ \circ \eta_2(1645) \\ \circ \omega_1(1670) \\ \circ \pi_2(1670) \\ \end{array} $		• $\phi(2170)$ $f_0(2220)$ $f_J(2220)$ $r_J(2220)$ • $f_2(2220)$ • $f_2(2230)$ • $f_2(2300)$ $f_4(2300)$ $f_0(2330)$ • $f_2(2340)$ $\rho_5(2350)$ X(2370) $f_6(2510)$ OTHEFF Further St.	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0.5 \\ 0.$	$\frac{1/2(5^{-})}{1/2(4^{-})}, \frac{2}{2(7^{+})}$ $\frac{1}{1/2(0^{-})}, \frac{1}{1/2(0^{-})}, \frac{1}{1/2(1^{-})}, \frac{1}{1/2(1^{-})}, \frac{1}{1/2(1^{+})}, \frac{1}{1/2(1^{+})}, \frac{1}{1/2(2^{+})}, \frac{1}{1/2(1^{-})}, \frac{1}{1/2(1^{-})}, \frac{1}{1/2(2^{-})}, $	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $B_2(5970)$ • B_5° • B_5° • B_5° • B_5° • $B_{51}(5830)^0$ • $B_{52}^{\circ}(5840)^0$ $B_{52}^{\circ}(5840)^0$ BOTTOM, $C_{(B=C)}^{\circ}$ • B_c^{+} • $B_c(2S)^{\pm}$ (+ possibly no	$\frac{1}{2(2^{-})}$ $\frac{1}{2(?^{2})}$ $\frac{1}{2(?^{2})}$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$ $?(?^{2})$ CHARMED $= \pm 1$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $\frac{1}{2}$ for $q\bar{q}$ states)	$\begin{array}{c} \psi(460)\\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \\ \psi(460)\\ \psi(4700) \\ \hline \\ \psi(4700) \\ $	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array}$
$ \begin{array}{l} \circ \rho(1450) \\ \circ \eta(1475) \\ \circ f_0(1500) \\ f_1(1510) \\ \circ f'_2(1525) \\ f_2(1565) \\ \rho(1570) \\ h_1(1595) \\ \circ \pi_1(1600) \\ \circ a_1(1640) \\ f'_2(1640) \\ \circ \eta_2(1645) \\ \circ \omega_1(1670) \\ \circ \pi_2(1670) \\ \end{array} $		• φ(2170) f ₀ (2220) f ₁ (2220) η (2225) $\rho_3(2250)$ • f ₂ (2300) f ₀ (2330) • f ₂ (2340) $\rho_5(2350)$ χ (2370) f ₆ (2510) OTHEF Further St.	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(4++) 0+(0++) 0+(2	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0.5 \\ 0.$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 \pm 1, 0)$ • B_5^{0} • B_5^{0} • B_5^{0} • $B_{51}(5830)^{0}$ • $B_{52}^{0}(5840)^{0}$ $B_{52}^{0}(5840$	$\frac{1}{2(2^{-})}$ $\frac{1}{2(?^{2})}$ $\frac{1}{2(?^{2})}$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$ $?(?^{2})$ CHARMED $= \pm 1$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0^{+}(0^{-}+)$	$\begin{array}{c} \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \psi(4700) \\ \psi(4700)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \\ \hline \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^- (2) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (1 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (1 + +) \\ 0^- (1) \\ 0^+ (1 + +) \end{array}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f_2'(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2'(1640)$ • $\eta_2(1645)$ • $\omega(1650)$ • $\omega_3(1670)$ • $\pi_2(1670)$		 φ(2170) f₀(2200) f₀(2220) f₂(2220) φ₃(2250) f₂(2300) f₂(2300) f₂(2340) φ₅(2350) X(2370) f₆(2510) OTHEF Further St. 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0.5 \\ 0.$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \end{array}$	• $B_2(3147)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 \pm 1, 0)$ • B_5^{0} • B_5^{0} • B_5^{0} • $B_{51}(5830)^{0}$ • $B_{52}^{0}(5840)^{0}$ $B_{52}^{0}(5840$	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $\frac{5}{5} = \pm 1$ $0(0^{-})$ $0(1^{-})$ $2(2^{+})$ $0(1^{+})$ $0(2^{+})$ $2(2^{+})$ $2(2^{+})$ $2(2^{+})$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0^{+}(0^{-})$ $0^{-}(1^{-})$ $0^{-}(1^{-})$	$\begin{array}{c} \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \psi(4700) \\ \psi(4700)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^- (2) \\ 0^- (0 - +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^+ (2 + +) \\ 0^+ (2 + +) \end{array}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f_2'(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2'(1640)$ • $\eta_2(1645)$ • $\omega_3(1670)$ • $\pi_2(1670)$		 φ(2170) f₀(2200) f₁(2220) f₂(2220) φ₂(2250) f₂(2300) f₂(2300) f₂(2340) φ₅(2350) X(2370) f₆(2510) OTHEF Further State 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(4++) 0+(0++) 0+(2++) 1+(5) ? [?] (? [?]) 0+(6++) 2LIGHT ates	$\begin{array}{c} K_5^*(2380)\\ K_4(2500)\\ K(3100)\\ \hline\\ CHARM\\ (C = \pm \\ \bullet D^0\\ \bullet D^*(2007)^0\\ \bullet D^*(2010)^\pm\\ \bullet D_0^*(2300)\\ \bullet D_1(2420)\\ \bullet D_1(2420)$	$\begin{array}{c} 1/2(5^{-}) \\ 1/2(4^{-}) \\ ?'(?^{?}) \\ \end{array}$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 \pm 1, 0)$ • B_5^{0} • B_5^{0} • B_5^{0} • B_5^{0} • $B_{52}(5840)^{0}$	$\frac{1}{2(2^{-})}$ $\frac{1}{2(?^{2})}$ $\frac{1}{2(?^{2})}$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{2})$ $0(1^{+})$ $0(2^{+})$ $?(?^{2})$ CHARMED $= \pm 1$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0^{+}(0^{-}+)$ $0^{-}(1^{-}-)$ $0^{+}(0^{+}+)$	$\begin{array}{c} \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \psi(4700) \\ \psi(4700)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \\ \hline \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1 -$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f_2'(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$ • $\eta_2(1645)$ • $\omega_3(1670)$ • $\pi_2(1670)$		 φ(2170) f₀(2200) f₁(2220) r₂(2250) f₂(2300) f₂(2300) f₂(2340) ρ₅(2350) X(2370) f₆(2510) OTHEF Further State 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(4++) 0+(0++) 0+(2++) 1+(5) ?'(?') 0+(6++) CLIGHT ates	$\begin{array}{c} K_5^*(2380)\\ K_4(2500)\\ K(3100)\\ \hline \\ CHARM\\ (C = \pm \\ 0.5 \\ $	$1/2(5^{-})$ $1/2(4^{-})$?(??) HED $1/2(0^{-})$ $1/2(0^{-})$ $1/2(1^{-})$ $1/2(1^{-})$ $1/2(1^{+})$ $1/2(1^{+})$ $1/2(2^{+})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 = \pm 1, -1)$ • B_5^0 • B_5^0 • B_5^* • $X(5568)^{\pm}$ • $B_{51}(5830)^0$ • $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ • $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ • $B_{52}^*(5840)^0$ • $B_{52}^*(5840)^0$	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{?})$ $0(1^{+})$ $0(2^{+})$ $?(?^{?})$ CHARMED $= \pm 1$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0^{+}(0^{-}+)$ $0^{-}(1^{-}-)$ $0^{+}(0^{+}+)$ $0^{-}(1^{+}+)$ $0^{-}(1^{+}+)$ $0^{-}(1^{+}+)$	$\begin{array}{c} \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \psi(4700) \\ \psi(4700)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \end{array} \\ \hline \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (1 + -) \\ 0^+ (1) \\ 1^+ (1 + -) \end{array}$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f'_2(1525)$ • $f_2(1565)$ • $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$ • $\eta_2(1645)$ • $\omega_3(1670)$ • $\pi_2(1670)$	$ \begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2-+)\\ 0-(1)\\ 1-(2-+)\\ 1-(2-+) \end{array} $	 φ(2170) f₀(2200) f₁(2220) r₂(2250) f₂(2300) f₂(2300) f₂(2340) ρ₅(2350) X(2370) f₆(2510) OTHEF Further State 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(0++) 0+(0++) 0+(0++) 0+(2++) 1+(5) ?'(?') 0+(6++) CLIGHT ates	$\begin{array}{c} K_5^*(2380)\\ K_4(2500)\\ K(3100)\\ \hline \\ CHARM\\ (C = \pm \\ \bullet D^0\\ \bullet D^*(2007)^0\\ \bullet D^*(2010)^\pm\\ \bullet D_0^*(2300)\\ \bullet D_1(2420)\\ \bullet D_1(2420$	$1/2(5^{-})$ $1/2(4^{-})$?(??) HED $1/2(0^{-})$ $1/2(0^{-})$ $1/2(1^{-})$ $1/2(1^{-})$ $1/2(1^{+})$ $1/2(1^{+})$ $1/2(2^{+})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 = \pm 1, -1)$ • B_5^0 • B_5^0 • B_5^* • $X(5568)^{\pm}$ • $B_{51}(5830)^0$ • $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ $B_{52}^*(5840)^0$ • $B_{52}^*(5840)^0$ • $B_{52}^*(5840)^$	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $?(?^{?})$ $0(1^{+})$ $0(2^{+})$ $?(?^{?})$ CHARMED $= \pm 1$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0^{+}(0^{-}+)$ $0^{-}(1^{-}-)$ $0^{+}(0^{+}+)$ $0^{-}(1^{+}-)$ $0^{+}(1^{+}+)$ $0^{-}(1^{+}-)$ $0^{+}(2^{+}+)$	$\begin{array}{c} \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \psi(460)\\ \psi(4700) \\ \psi(4700)\\ \psi(470)$	$\begin{array}{c} 0-(1)\\ 0+(0++)\\ \hline \\ \hline \\ \hline \\ 0-q\overline{q} \text{ states})\\ \hline \\ 0^+(0-+)\\ 0^-(1)\\ 0^+(0++)\\ 0^+(0++)\\ 0^-(1+-)\\ 0^+(2++)\\ 0^-(1)\\ 0^+(2++)\\ 0^-(1)\\ 0^+(1++)\\ 0^-(1)\\ 0^+(1++)\\ 0^-(1)\\ 0^+(1++)\\ 0^-(1)\\ 1^+(1+-)\\ 1^+(1+-)\\ 1^+(1+-)\\ 1^+(1+-)\\ 1^+(1+-)\\ 1^+(1+-)\\ 0^+(2++)\\ 0^-(1)\\ 0^+(1++)\\ 0^-(1)\\ 0^+(1++)\\ 0^-(1)\\ 0^+(1++)\\ 0^-(1)\\ 0^+(1++)\\ 0^-(1)\\ 0^+(1+-)\\ 0^+($
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f'_2(1525)$ • $f_2(1565)$ • $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$ • $\eta_2(1645)$ • $\omega(1650)$ • $\omega_3(1670)$ • $\pi_2(1670)$		 φ(2170) f₀(2200) f₁(2220) r₂(2250) f₂(2300) f₂(2300) f₂(2340) ρ₅(2350) X(2370) f₆(2510) OTHEF Further State 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(4++) 0+(0++) 0+(2++) 1+(5) ? [?] (? [?]) 0+(6++) CLIGHT ates	$\begin{array}{c} K_5^*(2380) \\ K_4(2500) \\ K(3100) \\ \hline \\ CHARM \\ (C = \pm \\ 0 \\ D^{\pm} \\ 0 \\ D^{\pm} \\ 0 \\ D^{\pm} \\ 2007)^{0} \\ D^{\pm} \\ 2007)^$	$1/2(5^{-})$ $1/2(4^{-})$?(??) HED $1/2(0^{-})$ $1/2(0^{-})$ $1/2(1^{-})$ $1/2(1^{-})$ $1/2(1^{+})$ $1/2(1^{+})$ $1/2(2^{+})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 = \pm 1, -1)$ • B_5^0 • B_5^0 • B_5^* • $X(5568)^{\pm}$ • $B_{51}(5830)^0$ • $B_{52}^*(5840)^0$	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $2^{(?)}$ $0(1^{+})$ $0(2^{+})$ $2^{(?)}$ CHARMED $= \pm 1$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0^{+}(0^{-}+)$ $0^{-}(1^{-}-)$ $0^{+}(0^{+}+)$ $0^{-}(1^{+}-)$ $0^{+}(1^{+}+)$ $0^{-}(2^{+}+)$ $0^{+}(2^{+}+)$ $0^{+}(2^{+}+)$	$\begin{array}{c} \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \psi(460)\\ \psi(4700) \\ \psi(4700) \\ \psi(4700)\\ \psi(470)\\ \psi(4700)\\ \psi(470)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \end{array} \\ \hline \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (1 + +) \\ 0^- (1) \\ 0^+ (1 + +) \\ 0^- (1) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^- (1) \\ 1^+ (1 + -) \\ 1^+ (1) \\ 1^+ (1) \\ 2^- (1) \\ 0^$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f'_2(1525)$ • $f_2(1565)$ • $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$ • $\eta_2(1645)$ • $\omega(1650)$ • $\omega_3(1670)$ • $\pi_2(1670)$	$ \begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2++)\\ 0-(1)\\ 0-(3)\\ 1-(2-+) \end{array} $	 φ(2170) f₀(2200) f₁(2220) r₂(2250) f₂(2300) f₂(2300) f₀(2330) f₂(2340) ρ₅(2350) X(2370) f₆(2510) OTHEF Further State 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(0++) 0+(0++) 0+(0++) 0+(0++) 0+(6++) RLIGHT ates	$\begin{array}{c} K_5^*(2380)\\ K_4(2500)\\ K(3100)\\ \hline\\ CHARM\\ (C = \pm \\ \bullet D^0\\ \bullet D^*(2007)^0\\ \bullet D^*(2010)^\pm\\ \bullet D_0^*(2300)\\ \bullet D_1(2420)\\ \bullet D_1(2420)$	$1/2(5^{-})$ $1/2(4^{-})$?(??) HED $1/2(0^{-})$ $1/2(0^{-})$ $1/2(1^{-})$ $1/2(1^{-})$ $1/2(1^{+})$ $1/2(1^{+})$ $1/2(2^{+})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$	• $B_2(3747)$ $B_3(5840)$ • $B_3(5970)$ BOTTOM, $E_3(B_2 = \pm 1, 0)$ • B_3^c • B_5^c • B_5^c • $B_{51}(5830)^0$ • $B_{52}^c(5840)^0$ $B_{52}^c(5840)^0$ $B_{52}^c(5840)^0$ $B_{52}^c(5840)^0$ $B_{52}^c(5840)^0$ • $B_{52}^c(5840)^0$ • $B_{52}^c(58$	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $2^{(?)}$ $0(1^{+})$ $0(2^{+})$ $2^{(?)}$ CHARMED $= \pm 1$ $0(0^{-})$ $0(0^{-})$ $0(0^{-})$ $0^{+}(0^{-}+)$ $0^{-}(1^{-}-)$ $0^{+}(0^{+}+)$ $0^{-}(1^{+}-)$ $0^{+}(2^{+}+)$ $0^{-}(1^{-}-)$ $0^{+}(2^{-}+)$ $0^{-}(1^{-}-)$ $0^{+}(2^{-}+)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$ $0^{-}(1^{-}-)$	$\begin{array}{c} \psi(4600)\\ \psi(4600)\\ \chi_{c0}(4700) \end{array} \\ \hline \\ \psi(4600)\\ \psi(4600)\\ \psi(4600)\\ \psi(4700) \end{array} \\ \\ \hline \\ \psi(4700)\\ \psi$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \end{array} \\ \hline \\ 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (1 + +) \\ 0^- (1) \\ 0^+ (1 + +) \\ 0^- (1) \\ 0^+ (1 + -) \\ 1^+ (1 + -) \\ 1^+ (1 + -) \\ 1^+ (1) \\ 0^- (1) \\ 0^$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f_2'(1525)$ • $f_2(1565)$ • $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$ • $\eta_2(1645)$ • $\omega(1650)$ • $\omega_3(1670)$ • $\pi_2(1670)$	$ \begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2++)\\ 0-(1)\\ 1-(2-+)\\ 1-(2-+) \end{array} $	 φ(2170) f₀(2200) f₁(2220) r₂(2250) f₂(2300) f₂(2300) f₀(2330) f₂(2340) ρ₅(2350) X(2370) f₆(2510) OTHEF Further State 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(4++) 0+(0++) 0+(2++) 1+(5) ? [?] (? [?]) 0+(6++) 2LIGHT ates	$\begin{array}{c} K_5^*(2380)\\ K_4(2500)\\ K(3100)\\ \hline\\ CHARM\\ (C = \pm \\ \bullet D^0\\ \bullet D^*(2007)^0\\ \bullet D^*(2010)^\pm\\ \bullet D_0^*(2300)\\ \bullet D_1(2420)\\ \bullet D_1(2420)$	$1/2(5^{-})$ $1/2(4^{-})$?(??) HED $1/2(0^{-})$ $1/2(0^{-})$ $1/2(1^{-})$ $1/2(1^{-})$ $1/2(1^{+})$ $1/2(1^{+})$ $1/2(2^{+})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$	• $B_2(374)$ $B_J(5840)$ • $B_J(5970)$ BOTTOM, $E_{(B = \pm 1, 1)}$ • B_5° • B_5° • B_5° • B_5° • $B_{51}(5830)^0$ • $B_{52}^{\circ}(5840)^0$ $B_{52}^{$	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $2(2^{+})$ $0(2^{+})$ $2(2^{+})$ $0(0^{-$	$\begin{array}{c} \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \psi(460)\\ \psi(460)$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \\ \hline 0 + (0 - +) \\ 0 - (1) \\ 0 + (0 + +) \\ 0 - (1) \\ 0 + (2 + +) \\ 0 - (1) \\ 0 - (2) \\ 0 - (1) \\ 0 - (2) \\ 0 - (1) \\ 0 - (1) \\ 0 + (2 + +) \\ 0 - (1) \\ 0 - (1) \\ 0 + (1 + +) \\ 0 - (1) \\ 0 - (1) \\ 1 + (1 + -) \\ 1 + (1 + -) \\ 1 + (1 + -) \\ 1 - (1) \\ 0 - (1$
• $\rho(1450)$ • $\eta(1475)$ • $f_0(1500)$ • $f_1(1510)$ • $f_2'(1525)$ • $f_2(1565)$ $\rho(1570)$ • $h_1(1595)$ • $\pi_1(1600)$ • $a_1(1640)$ • $f_2(1640)$ • $\eta_2(1645)$ • $\omega(1650)$ • $\omega_3(1670)$ • $\pi_2(1670)$	$ \begin{array}{c} 1+(1)\\ 0+(0-+)\\ 0+(0++)\\ 0+(1++)\\ 0+(2++)\\ 1+(1)\\ 0-(1+-)\\ 1-(1-+)\\ 1-(1++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2++)\\ 0+(2++)\\ 0-(1)\\ 1-(2-+)\\ 1-(2-+)\\ \end{array} $	 φ(2170) f₀(2200) f₁(2220) r₂(2250) f₂(2300) f₂(2300) f₀(2330) f₂(2340) ρ₅(2350) X(2370) f₆(2510) OTHEF Further State 	0-(1) 0+(0++) 0+(2++ or 4++) 0+(0-+) 1+(3) 0+(2++) 0+(2++) 0+(4++) 0+(0++) 0+(2++) 1+(5) ? [?] (? [?]) 0+(6++) CLIGHT ates	$\begin{array}{c} K_5^*(2380)\\ K_4(2500)\\ K(3100)\\ \hline\\ CHARM\\ (C = \pm\\ 0.000\\ D^{\pm}\\ 0.000\\ D^{\pm}(2007)^{0}\\ D^{\pm}(2010)^{\pm}\\ D^{\pm}(2010)^{\pm}\\ D^{\pm}(2010)^{\pm}\\ D^{\pm}(2010)^{\pm}\\ D^{\pm}(2420)\\ D_{1}(2420)\\ D_{1}(2420)\\ D_{1}(2420)\\ D_{1}(2420)^{0}\\ D^{\pm}(2600)^{0}\\ D^{\pm}(2640)^{\pm}\\ D_{2}(2740)^{0}\\ D^{\pm}(2640)^{\pm}\\ D_{2}(2740)^{0}\\ D^{\pm}(2750)\\ D^{\pm}(2760)^{0}\\ D(3000)^{0}\\ \end{array}$	$1/2(5^{-})$ $1/2(4^{-})$?(??) HED $1/2(0^{-})$ $1/2(0^{-})$ $1/2(1^{-})$ $1/2(1^{-})$ $1/2(1^{+})$ $1/2(1^{+})$ $1/2(2^{+})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$ $1/2(2^{-})$	• $B_2(3747)$ $B_j(5840)$ • $B_j(5970)$ BOTTOM, $E_{(B = \pm 1, 1)}$ • B_s^0 • B_s^* • $X(5568)^{\pm}$ • $B_{s1}(5830)^0$ • $B_{s2}^*(5840)^0$ $B_{s3}^*(5850)$ BOTTOM, $C_{(B = C)}$ • B_c^+ • $B_c(2S)^{\pm}$ (+ possibly noise of the second	$\frac{1}{2}(2^{-})$ $\frac{1}{2}(2^{?})$ $\frac{1}{2}(2^{?})$ STRANGE $S = \pm 1$ $0(0^{-})$ $0(1^{-})$ $2^{?}(2^{-})$ $0(1^{+})$ $0(2^{+})$ $2^{?}(2^{-})$ $0(0^{-})$ $0^{-}(1^{-})$ $0^{-}(1^{-})$ $0^{-}(1^{-})$ $0^{-}(1^{-})$ $0^{-}(1^{-})$ $0^{-}(2^{-})$ $0^{-}(2^{-})$	$\begin{array}{c} \psi(4600)\\ \psi(4600)\\ \chi_{c0}(4700) \\ \hline \\ \\ \hline \\ \psi(460)\\ \chi_{c0}(4700) \\ \hline \\ \\ \psi(460)\\ \psi(4700) \\ \hline \\ \\ \psi(4700)\\ \psi(4700)\\$	$\begin{array}{c} 0 - (1) \\ 0 + (0 + +) \end{array} \\ \hline \\ \hline \\ \hline \\ 0 - q \overline{q} \text{ states}) \end{array} \\ \hline 0^+ (0 - +) \\ 0^- (1) \\ 0^+ (0 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^+ (1 + +) \\ 0^- (1) \\ 0^+ (1 + -) \\ 0^+ (2 + +) \\ 0^- (1) \\ 0^- (1) \\ 1^+ (1 + -) \\ 1^+ (1) \\ 0^- (1) \\ 0^- (1) \\ 0^- (1) \\ 0^- (1) \end{array}$

1/2+ **** 3/2+ **** 1/2+ **** Ξ++ *** 1/2+ **** $\Delta(1232)$ 5 =0 1/2+ **** 3/2+ **** 1/2+ **** 1/2+ **** *∆*(1600) Σ^0 =-1/2+ **** 1/2 **** 3/2+ 1/2+ **** **** Λb 1/2+ *** N(1440) Σ- $\Xi(1530)$ $\Delta(1620)$ 3/2 **** 3/2 **** N(1520) $\Delta(1700)$ Σ(1385) 3/2+ **** $\Xi(1620)$ * $\Lambda_{b}(5912)^{0} 1/2^{-} ***$ 3/2 * 1/2 **** $1/2^{+}$ * *** $\Lambda_b(5920)^0$ $3/2^- ***$ N(1535) $\Delta(1750)$ $\Sigma(1580)$ $\Xi(1690)$ 1/2 **** 1/2 *** $1/2^{-}$ * Λ_b(6146)⁰ 3/2⁺ *** N(1650) *∆*(1900) Σ(1620) Ξ(1820) *** $3/2^{-}$ 5/2 **** 5/2+ **** 1/2+ *** Ab(6152)⁰ 5/2⁺ *** *** N(1675) $\Delta(1905)$ $\Sigma(1660)$ $\Xi(1950)$ 5/2+ **** 1/2+ **** 3/2 **** $\geq \frac{5}{2}$ *** 1/2+ *** Σ(1670) N(1680) $\Delta(1910)$ $\Xi(2030)$ Σb N(1700) 3/2 *** 3/2+ *** Σ(1750) 1/2 *** * Σ_{h}^{*} 3/2+ *** *∆*(1920) Ξ(2120) 5/2 *** 5/2 **** 1/2+ **** *** N(1710) $\Delta(1930)$ **Σ(1775)** Ξ(2250) ** $\Sigma_b(6097)^+$ 3/2+ **** *∆*(1940) 3/2 ** Σ(1780) 3/2+ * ** *** N(1720) $\Xi(2370)$ $\Sigma_{b}(6097)^{-1}$ 5/2+ ** 1/2+ *** 1/2+ ** 7/2+ **** N(1860) $\Delta(1950)$ **Σ(1880)** * Ξ(2500) Ξ 3/2- *** 5/2+ ** 1/2- ** Σ(1900) 1/2+ *** N(1875) $\Delta(2000)$ =0 $1/2^{-}$ * 3/2 *** 1/2+ *** 3/2+ **** N(1880) ∆(2150) Σ(1910) Ω^{-} $\Xi_{b}^{\prime}(5935)^{-} 1/2^{+} ***$ 1/2- **** 5/2+ **** 7/2 *** N(1895) $\Delta(2200)$ Σ(1915) $\Omega(2012)^{-}$? *** $\Xi_b(5945)^0$ $3/2^+$ *** 3/2+ **** 9/2+ ** Σ(1940) 3/2+ * *** N(1900) $\Delta(2300)$ $\Omega(2250)$ $\Xi_b(5955)^-$ 3/2⁺ *** 7/2+ ** N(1990) $\Delta(2350)$ 5/2- * Σ(2010) 3/2 * $\Omega(2380)^{-1}$ ** *** $\Xi_b(6227)^-$ 5/2+ ** 7/2+ **** 7/2+ * ** N(2000) ∆(2390) Σ(2030) $\Omega(2470)$ $\Xi_b(6227)^0$ *** 1/2+ **** 9/2" ** 5/2+ * 3/2+ * N(2040) ∆(2400) Σ(2070) $1/2^{+}$ *** Ω_{h}^{-} 11/2+ **** N(2060) 5/2 *** Σ(2080) 3/2+ * $\Lambda_{c}(2595)^{+} 1/2^{-} ***$ $\Delta(2420)$ $\Omega_{b}(6316)^{-}$ 1/2+ *** 13/2- ** 7/2 * N(2100) $\Delta(2750)$ Σ(2100) Ac(2625)+ 3/2- *** $\Omega_{b}(6330)^{-1}$ * N(2120) 3/2 *** ∆(2950) 15/2+ ** Σ(2160) 1/2- * $\Lambda_{c}(2765)^{+}$ Ω_b(6340)⁻ * 3/2+ * 7/2 **** $\Lambda_{c}(2860)^{+} 3/2^{+} ***$ N(2190) Σ(2230) * $\Omega_{b}(6350)^{-}$ 9/2+ **** 1/2+ **** *** $\Lambda_c(2880)^+ 5/2^+ ***$ Λ Σ(2250) N(2220) 9/2 **** 1/2 ** Λ ** *∧*_c(2940)⁺ 3/2[−] *** N(2250) Σ(2455) $P_{c}(4312)^{+}$ * 1/2 **** 1/2+ ** ** $\Sigma_c(2455)$ 1/2⁺ **** N(2300) A(1405) $\Sigma(2620)$ $P_{C}(4380)^{+}$ * 3/2" **** 3/2+ *** N(2570) 5/2 ** A(1520) Σ(3000) * $\Sigma_{c}(2520)$ * $P_{c}(4440)^{+}$ 1/2+ **** 11/2" *** A(1600) N(2600) Σ(3170) *** $\Sigma_{c}(2800)$ $P_{c}(4457)^{+}$ 13/2+ ** 1/2 **** A(1670) 1/2+ *** N(2700) 3/2 **** A(1690) 1/2+ **** A(1710) $1/2^{+}$ * 1/2+ *** 1/2- *** A(1800) 1/2+ *** 1/2+ *** A(1810) 3/2+ *** $\Xi_{c}(2645)$ A(1820) 5/2+ **** $\Xi_{c}(2790)$ 1/2 *** 5/2- **** A(1830) *** $\Xi_{c}(2815)$ $3/2^{-}$ A(1890) 3/2+ **** ** $\Xi_{c}(2923)$ A(2000) $1/2^{-}$ * $\Xi_{c}(2930)$ ** A(2050) 3/2 * *** $\Xi_{c}(2970)$ 3/2+ * A(2070) $\Xi_{c}(3055)$ *** 5/2 * A(2080) *** $\Xi_{c}(3080)$ 7/2+ ** A(2085) $\Xi_{c}(3123)$ A(2100) 7/2 **** Ω^0 $1/2^{+}$ *** 5/2+ *** A(2110) $\Omega_c(2770)^0 3/2^+$ *** 3/2 * A(2325) $\Omega_{c}(3000)^{0}$ *** A(2350) 9/2+ *** *** $\Omega_{c}(3050)^{0}$ ** A(2585) $\Omega_{c}(3065)^{0}$ *** *** $\Omega_{c}(3090)^{0}$ $\Omega_{c}(3120)^{0}$ ***

This short table gives the name, the quantum numbers (where known), and the status of baryons in the Review. Only the baryons with 3- or 4-star status are included in the Baryon Summary Table. Due to insufficient data or uncertain interpretation, the other entries in the table

are not established baryons. The names with masses are of baryons that decay strongly. The spin-parity J^P (when known) is given with each

particle. For the strongly decaying particles, the J^P values are considered to be part of the names.

**** Existence is certain, and properties are at least fairly well explored.

*** Existence ranges from very likely to certain, but further confirmation is desirable and/or quantum numbers, branching fractions, etc. are not well determined.

** Evidence of existence is only fair.

* Evidence of existence is poor.

1 e

STRONG INTERACTIONS :: FUNDAMENTAL PARTICLES

- ver the 40-60s [of last century], as particle colliders became available, a large number of particles was discovered [many as resonances] experiencing the strong interaction
 - a seriously explored possibility was that ALL of them were fundamental [this went well with 60s political views]
 - clearly not a very elegant solution
- Gell-Mann and Zweig [1964] proposed that all hadrons known by then were composed of more elementary constituents [named quarks after the obscure line '-Three quarks for Muster Mark!' in James Joyce's obscure book Finnegans Wake]
 - these 'hypothetical' quarks would come in 3 flavours [u(p),d(own),s(trange)] with the respective anti-particles [as they were fermions]

THE EIGHTFOLD WAY



by combining the quarks and anti-quarks in all possible ways it was possible to accommodate all known baryons and mesons known at the time and PREDICT the existence of a few others [later observed]

THE EIGHTFOLD WAY :: A CLEAR PROBLEM



- states [particles] predicted and observed have 3 quarks of same flavour [uuu, ddd, sss]
- Spin-1/2 fermions in the same quantum state is problematic to say the least [Pauli exclusion principle]
 - solved by introducing a new quantum number [a charge] called colour [r,g,b]
 - ➤ all observed particles must be white
 - colour is the conserved charge of the strong interactions
 - ► 3 charges :: SU(3) gauge symmetry

WHERE ARE THE QUARKS

- although the model with 3 quarks [now we know there are 6] each in one of three possible colour states worked well to describe hadron zoology
 - free quarks had not [and have not] been observed
 - > do they exist or are simply a convenient mathematical construction?

FRIEDMAN, KENDALL, TAYLOR [SLAC-MIT EXPERIMENTS 1968- :: NOBEL 1990]



- in electron-proton scattering experiments the exchanged [virtual] photon acts as a microscope resolving structures with size ~1/Q²
 - for low Q² the proton is seen as a whole
 - increasing Q² probes the proton internal structure [if any]
 - experimental results at sufficiently high Q² consistent with the existence of 3 quarks in the proton

WHY ARE QUARKS NEVER FREE ?

Iook at the QCD Lagrangian [built like we did for QED but now imposing a SU(3) gauge symmetry]

QCD IN ONE SLIDE

:: each quark flavour [u,d,c,s,b,t] exists in 3 colours [r,g,b]

:: quark carries one colour index :: fundamental representation of SU(3) [triplet]



:: need to introduce gauge field [gluon] to fulfil gauge invariance:: gluon carries two colour indices :: adjoint representation of SU(3) [octet]

:: once new field available, include all further gauge invariant terms

$$\mathcal{L}_{QCD} = \sum_{\text{flavours}} \bar{\psi}_a \left(\left(i\gamma^{\mu} \partial_{\mu} - m \right) \delta_{ab} - g_{\mu} \gamma^{\mu} t^C_{ab} A^C_{\mu\nu} \right) \psi_b - \frac{1}{4} F^A_{\mu\nu} F^{\mu\nu,A} F^{\mu\mu,A} F^{\mu\nu,A} F^{\mu\mu,A} F^{\mu\mu,A} F^{\mu\mu,A} F^{\mu\mu,A} F^{\mu\mu,A} F^{\mu\mu,A} F^{\mu\mu,A} F^{\mu\mu,A}$$

Lagrangian structure fixed by requirement of $SU(3)_{colour}$ gauge symmetry

WELL, TWO

$$\mathcal{L}_{QCD} = -\frac{1}{4} F^{A}_{\mu\nu} F^{\mu\nu,A} + \sum_{\text{flavours}} \bar{\psi}_a \Big((i\gamma^{\mu}\partial_{\mu} - m) \delta_{ab} - g_s \gamma^{\mu} t^{C}_{ab} A^{C}_{\mu} \Big) \psi_b$$

$$F^{A}_{\mu\nu} = \partial_{\mu} \mathcal{A}^{A}_{\nu} - \partial_{\nu} \mathcal{A}^{A}_{\nu} - g_s f_{ABC} \mathcal{A}^{B}_{\mu} \mathcal{A}^{C}_{\nu} \qquad [t^{A}, t^{B}] = i f_{ABC} t^{C}$$

• gluon propagator + gluon self-interactions





Quark masses

b

Up	2.3 MeV	Charm	1275 MeV	Тор	173 GeV
Down	4.8 MeV	Strange	95 MeV	Bottom	4180 MeV

· •

$\mathcal{ASYMPTOTIC FREEDOM AND CONFINEMENT}$ $\mathcal{L}_{QCD} = -\frac{1}{4} F^{A}_{\mu\nu} F^{\mu\nu,A} + \sum_{\text{flavours}} \bar{\psi}_a \Big((i\gamma^{\mu}\partial_{\mu} - m) \delta_{ab} - g_s \gamma^{\mu} t^{C}_{ab} A^{C}_{\mu} \Big) \psi_b$

- renormalization [cancellation of divergences in higher order corrections] makes the coupling scale dependant
- ✓ self-interacting gauge fields lead to asymptotic freedom

:: quarks and gluon can only behave freely at high momentum scales [small distances] thus always observed confined within hadrons



WHY ARE QUARKS NEVER FREE ?

Iook at the QCD Lagrangian [built like we did for QED but now imposing a SU(3) gauge symmetry]

$$\mathcal{L}_{QCD} = -\frac{1}{4} F^{a}_{\mu\nu} F^{\mu\nu}_{a} + \bar{\psi}_{i} (i\gamma^{\mu}D_{\mu} - m)_{ij} \psi_{j}$$

$$F^{a}_{\mu} = \partial_{\mu}A^{a} - \partial_{\mu}A^{a}_{\mu} - (gf^{abc}A^{b}_{\mu}A^{c})$$

$$D_{\mu} = \partial_{\mu} + igA^{a}_{\mu}T^{a}$$
gauge bosons [gluons] self-interact unlike photons in electrodynamics

self-coupling of gluons leads makes [renormalized] coupling grow with increasing distance [confinement and asymptotic freedom]

Gross, Politzer, Wilczec [1973 :: Nobel 2004]

O problema: UNIFICATION OF FUNDAMENTAL INTERACTIONS

- Electricity and Magnetism [Maxwell 1873]
- weak interaction [Fermi 1934]
 - non-renormalizable [divergent at high energies]
- gauge invariance [Yang & Mills 1954]
 - 1930-60 :: search for gauge theories that unify EM and weak interaction (at this point it was not clear at all that strong interactions would fit in the QFT language)
 - SU(2)⊗U(1) symmetry [Glashow 1961]
 - spontaneous symmetry breaking [Weinberg & Salam 1967]

massless [Goldstone] gauge bosons which would lead to infinite range forces acquire mass through a simple mechanism

Englert-Brout-Higgs-Guralnik-Hagen-Kibble [1964] mechanism



O problema:

UNIFICATION OF FUNDAMENTAL INTERACTIONS

- Electricity and Magnetism [Maxwell 1873]
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 - SU(2)⊗U(1) symmetry [Glashow 1961]
 - quebra espontânea [Weinberg & Salam 1967]

bosões de gauge [mediadores da interacção] com massa nula [Goldstone] :: forças de alcance infinito

forma [a mais simples] de atribuir massa aos bosões de gauge [1964]



1964

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PHYSICAL REVIEW LETTERS

31 August 1964

BROKEN SYMMETRY AND THE MASS OF GAUGE VECTOR MESONS*

F. Englert and R. Brout Faculté des Sciences, Université Libre de Bruxelles, Bruxelles, Belgium (Received 26 June 1964)

Volume 13, Number 16

PHYSICAL REVIEW LETTERS

19 October 1964

BROKEN SYMMETRIES AND THE MASSES OF GAUGE BOSONS

Peter W. Higgs Tait Institute of Mathematical Physics, University of Edinburgh, Edinburgh, Scotland (Received 31 August 1964)

the only mentioning that the spontaneous symmetry breaking mechanism implies the existence of a scalar boson

Volume 13, Number 20	PHYSICAL REVIEW LETTERS	16 November 1964
GLOB	AL CONSERVATION LAWS AND MASSLESS PARTICLI	ES*
:	G. S. Guralnik, [†] C. R. Hagen, [‡] and T. W. B. Kibble Department of Physics, Imperial College, London, England (Received 12 October 1964)	

SPONTANEOUS SYMMETRY BREAKING

simple example with two real scalar fields φ₁, φ₂ [or a complex valued scalar field]

$$\begin{split} \mathcal{L} &= \mathcal{T}[\phi_1] + \mathcal{T}[\phi_2] - \mathcal{U}[\phi_1, \phi_2] \\ &\qquad \mathcal{U}[\phi_1, \phi_2] = -\frac{1}{2}\mu^2(\phi_1^2 + \phi_2^2) + \frac{1}{4}\lambda^2(\phi_1^2 + \phi_2^2)^2 \\ \text{select a minimum (e.g., } \Phi_1 = \mu/\lambda; \ \Phi_2 = 0) \end{split}$$

 symmetry is spontaneously broken :: vacuum is not invariant for symmetries of the lagrangian



SPONTANEOUS SYMMETRY BREAKING

simple example with two real scalar fields φ₁, φ₂ [or a complex valued scalar field]

$$\begin{split} \mathcal{L} &= \mathcal{T}[\phi_1] + \mathcal{T}[\phi_2] - \mathcal{U}[\phi_1, \phi_2] \\ & \mathcal{U}[\phi_1, \phi_2] = -\frac{1}{2}\mu^2(\phi_1^2 + \phi_2^2) + \frac{1}{4}\lambda^2(\phi_1^2 + \phi_2^2)^2 \\ \text{lect a minimum (e.g., } \Phi_1 = \mu/\lambda; \ \Phi_2 = 0) \end{split}$$

- symmetry is spontaneously broken :: vacuum is not invariant for symmetries of the lagrangian
- expand around the minimum

se

 η

$$\equiv \phi_1 - \frac{\mu}{\lambda} \qquad \xi \equiv \phi_2$$

$$\mathcal{L} = \mathcal{T}[\eta] - \mu^2 \eta^2 + \mathcal{T}[\xi] - 0 - \mu \lambda (\eta^3 + \eta \xi^2) - \frac{\lambda^2}{4} (\eta^4 + \xi^4 + 2\eta^2 \xi^2) + \frac{\mu^4}{4\lambda^2}$$
massive **n** field massless **ξ** field

 $\mathcal{L} = \mathcal{T}[\phi_1] + \mathcal{T}[\phi_2] - \mathcal{U}[\phi_1, \phi_2], \quad \mathcal{U}[\phi_1, \phi_2] = -\frac{1}{2}\mu^2 \left(\phi_1^2 + \phi_2^2\right) + \frac{1}{4}\lambda^2 \left(\phi_1^2 + \frac{1}{4}\lambda^2\right) + \frac{$

- spontaneous symmetry breaking is an universal phenomenon
 - occurs, for example, in a system of magnetic dipoles $\eta \equiv \phi_1 \mu/\lambda, \ \xi \equiv \phi_2 \Longrightarrow$



THE [...] - HIGGS - [...] MECHANISM

- gauge theory (i.e., with a local symmetry) for a complex scalar field $\Phi=\Phi_1+i\Phi_2$
- [transverse] massless gauge field A_{μ}
- gauge symmetry $\Phi \longrightarrow e^{-i\theta(x)} \Phi$

•
$$A_{\mu} \rightarrow A_{\mu} + \partial_{\mu}\theta(x); D_{\mu} \rightarrow \partial_{\mu} + iqA_{\mu}; F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$$

$$\mathcal{L} = \frac{1}{2}(D_{\mu}\phi)^{*}(D^{\mu}\phi) - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{2}\mu^{2}\phi^{*}\phi - \frac{1}{4}\lambda^{2}(\phi^{*}\phi)^{2}$$

expand around minimum

$$\eta \equiv \phi_1 - \frac{\mu}{\lambda} \qquad \xi \equiv \phi_2 \to 0 \quad \left(\theta = \arctan(\phi_2/\phi_1)\right)$$
$$\mathcal{L} = \frac{1}{2} (\partial_\mu \eta)^* (\partial^\mu \eta) - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \mu^2 \eta^2 + \frac{q^2 \mu^2}{2\lambda^2} A_\mu A^\mu + \mathcal{O}(3)$$
$$massive \text{ Higgs boson}$$

[adds longitudinal polarization dof]

IN SUPERCONDUCTORS

- Ginzburg-Landau explandro mecanismo off de Higgs:
 - photon acquires effective mass and penetration in the superconductor field has a range 1/m



fundamental interactions

Guilherme Milhano [LIP & IST, Lisbon] gmilhano@lip.pt





EW SECTOR [BEFORE SSB]

The Lagrangian for the electroweak interactions is divided into four parts before electroweak symmetry breaking

$$\mathcal{L}_{EW} = \mathcal{L}_g + \mathcal{L}_f + \mathcal{L}_h + \mathcal{L}_y.$$

The \mathcal{L}_q term describes the interaction between the three W particles and the B particle.

$$\mathcal{L}_{g} = -\frac{1}{4} W^{\mu\nu}_{a} W^{a}_{\mu\nu} - \frac{1}{4} B^{\mu\nu} B_{\mu\nu'}$$

where $W^{a\mu\nu}$ (a = 1, 2, 3) and $B^{\mu\nu}$ are the field strength tensors for the weak isospin and weak hypercharge fields.

 \mathcal{L}_f is the kinetic term for the Standard Model fermions. The interaction of the gauge bosons and the fermions are through the gauge covariant derivative.

where the subscript *i* runs over the three generations of fermions, *Q*, *u*, and *d* are the left-handed doublet, right-handed singlet up, and right handed singlet down quark fields, and *L* and *e* are the left-handed doublet and right-handed singlet electron fields.

The h term describes the Higgs field F.

$$\mathcal{L}_h = |D_\mu h|^2 - \lambda \left(|h|^2 - \frac{v^2}{2} \right)^2$$

The y term gives the Yukawa interaction that generates the fermion masses after the Higgs acquires a vacuum expectation value.

$$\mathcal{L}_y = -y_{uij}\epsilon^{ab} h_b^{\dagger} \overline{Q}_{ia} u_j^c - y_{dij} h \overline{Q}_i d_j^c - y_{eij} h \overline{L}_i e_j^c + h.c.$$

EW SECTOR [AFTER SSB]

The Lagrangian reorganizes itself after the Higgs boson acquires a vacuum expectation value. Due to its complexity, this Lagrangian is best described by breaking it up into several parts as follows.

$$\mathcal{L}_{EW} = \mathcal{L}_K + \mathcal{L}_N + \mathcal{L}_C + \mathcal{L}_H + \mathcal{L}_{HV} + \mathcal{L}_{WWV} + \mathcal{L}_{WWVV} + \mathcal{L}_Y$$

The kinetic term \mathcal{L}_K contains all the quadratic terms of the Lagrangian, which include the dynamic terms (the partial derivatives) and the mass terms (conspicuously absent from the Lagrangian before symmetry breaking)

$$\mathcal{L}_{K} = \sum_{f} \overline{f} (i\partial \!\!\!/ - m_{f}) f - \frac{1}{4} A_{\mu\nu} A^{\mu\nu} - \frac{1}{2} W^{+}_{\mu\nu} W^{-\mu\nu} + m^{2}_{W} W^{+}_{\mu} W^{-\mu}$$
$$- \frac{1}{4} Z_{\mu\nu} Z^{\mu\nu} + \frac{1}{2} m^{2}_{Z} Z_{\mu} Z^{\mu} + \frac{1}{2} (\partial^{\mu} H) (\partial_{\mu} H) - \frac{1}{2} m^{2}_{H} H^{2}$$

where the sum runs over all the fermions of the theory (quarks and leptons), and the fields $A_{\mu\nu}$, $Z_{\mu\nu}$, $W^-_{\mu\nu}$, and $W^+_{\mu\nu} \equiv (W^-_{\mu\nu})^{\dagger}$ are given as

 $X_{\mu\nu} = \partial_{\mu}X_{\nu} - \partial_{\nu}X_{\mu} + gf^{abc}X^{b}_{\mu}X^{c}_{\nu}$, (replace X by the relevant field, and f^{abc} with the structure constants for the gauge group).

The neutral current \mathcal{L}_N and charged current \mathcal{L}_C components of the Lagrangian contain the interactions between the fermions and gauge bosons.

$$\mathcal{L}_N = eJ_\mu^{em} A^\mu + \frac{g}{\cos\theta_W} (J_\mu^3 - \sin^2\theta_W J_\mu^{em}) Z^\mu,$$

where the electromagnetic current J_{μ}^{em} and the neutral weak current J_{μ}^3 are

$$J^{em}_{\mu} = \sum_{f} q_f \overline{f} \gamma_{\mu} f_{,}$$

and

$$J^3_{\mu} = \sum_f I^3_f \overline{f} \gamma_{\mu} \frac{1 - \gamma^5}{2} f$$

 q_f and I_f^3 are the fermions' electric charges and weak isospin.

The charged current part of the Lagrangian is given by

$$\mathcal{L}_C = -\frac{g}{\sqrt{2}} \left[\overline{u}_i \gamma^\mu \frac{1-\gamma^5}{2} M_{ij}^{CKM} d_j + \overline{\nu}_i \gamma^\mu \frac{1-\gamma^5}{2} e_i \right] W_\mu^+ + h.c$$

 \mathcal{L}_H contains the Higgs three-point and four-point self interaction terms.

$$\mathcal{L}_{H} = -\frac{gm_{H}^{2}}{4m_{W}}H^{3} - \frac{g^{2}m_{H}^{2}}{32m_{W}^{2}}H^{4}$$

 \mathcal{L}_{HV} contains the Higgs interactions with gauge vector bosons.

$$\mathcal{L}_{HV} = \left(gm_W H + \frac{g^2}{4}H^2\right) \left(W^+_\mu W^{-\mu} + \frac{1}{2\cos^2\theta_W}Z_\mu Z^\mu\right)$$

 \mathcal{L}_{WWV} contains the gauge three-point self interactions.

$$\mathcal{L}_{WWV} = -ig[(W^{+}_{\mu\nu}W^{-\mu} - W^{+\mu}W^{-}_{\mu\nu})(A^{\nu}\sin\theta_{W} - Z^{\nu}\cos\theta_{W}) + W^{-}_{\nu}W^{+}_{\mu}(A^{\mu\nu}\sin\theta_{W} - Z^{\mu\nu}\cos\theta_{W})]$$

 \mathcal{L}_{WWVV} contains the gauge four-point self interactions

$$\mathcal{L}_{WWVV} = -\frac{g^2}{4} \Big\{ [2W^+_{\mu}W^{-\mu} + (A_{\mu}\sin\theta_W - Z_{\mu}\cos\theta_W)^2]^2 \\ - [W^+_{\mu}W^-_{\nu} + W^+_{\nu}W^-_{\mu} + (A_{\mu}\sin\theta_W - Z_{\mu}\cos\theta_W)(A_{\nu}\sin\theta_W - Z_{\nu}\cos\theta_W)]^2 \Big\}$$

and \mathcal{L}_Y contains the Yukawa interactions between the fermions and the Higgs field.

$$\mathcal{L}_Y = -\sum_f \frac{gm_f}{2m_W} \overline{f} f H$$

Note the $\frac{1-\gamma^5}{2}$ factors in the weak couplings: these factors project out the left handed components of the spinor fields. This is why electroweak theory (after symmetry breaking) is commonly said to be a chiral theory.

IN THE STANDARD MODEL

- in the SM the Higgs mechanism [SSB of the gauge symmetry $SU(2) \otimes U(1) \rightarrow U(1)$ with a quartic [renormalizable] potencial
 - gives mass to the carriers of the weak force $[Z^0, W^{\pm}]$
 - leaves the carrier of EA force [v] massless Modelo Estandar electro-feble:
 - adds
 - a scalar massive particle [Higgs boson]
 - 2 parameters [μ/λ : vacuum expectation value: μ : Higgs mass] *U* = -¹/₂μ²φ^{*}φ + ¹/₄λ²(φ^{*}φ)², m_h = √2μħ/c, ¹/_λ = ^{mass}/_{gw}√ħc
 allows for fermion [leptons and quarks] mass terms [without gauge
 - simmetry violation] as couplings the Higgs field $\longrightarrow m_f c^2 = \alpha_f (\mu/\lambda)$

$$\mathcal{L}_{int} = -\alpha_f \bar{\psi}_f \psi_f \phi \Longrightarrow m_f = \alpha_f (\mu/\lambda)$$

MODELO STANDARD [EW+STRONG]

$$\begin{aligned} \mathcal{L}_{GWS} &= \sum_{f} (\bar{\Psi}_{f} (i\gamma^{\mu} \partial \mu - m_{f}) \Psi_{f} - eQ_{f} \bar{\Psi}_{f} \gamma^{\mu} \Psi_{f} A_{\mu}) + \\ &+ \frac{g}{\sqrt{2}} \sum_{i} (\bar{a}_{L}^{i} \gamma^{\mu} b_{L}^{i} W_{\mu}^{+} + \bar{b}_{L}^{i} \gamma^{\mu} a_{L}^{i} W_{\mu}^{-}) + \frac{g}{2c_{w}} \sum_{f} \bar{\Psi}_{f} \gamma^{\mu} (I_{f}^{3} - 2s_{w}^{2} Q_{f} - I_{f}^{3} \gamma_{5}) \Psi_{f} Z_{\mu} + \\ &- \frac{1}{4} |\partial_{\mu} A_{\nu} - \partial_{\nu} A_{\mu} - ie(W_{\mu}^{-} W_{\nu}^{+} - W_{\mu}^{+} W_{\nu}^{-})|^{2} - \frac{1}{2} |\partial_{\mu} W_{\nu}^{+} - \partial_{\nu} W_{\mu}^{+} + \\ &- ie(W_{\mu}^{+} A_{\nu} - W_{\nu}^{+} A_{\mu}) + ig' c_{w} (W_{\mu}^{+} Z_{\nu} - W_{\nu}^{+} Z_{\mu}|^{2} + \\ &- \frac{1}{4} |\partial_{\mu} Z_{\nu} - \partial_{\nu} Z_{\mu} + ig' c_{w} (W_{\mu}^{-} W_{\nu}^{+} - W_{\mu}^{+} W_{\nu}^{-})|^{2} + \\ &- \frac{1}{2} M_{\eta}^{2} \eta^{2} - \frac{g M_{\eta}^{2}}{8M_{W}} \eta^{3} - \frac{g'^{2} M_{\eta}^{2}}{32M_{W}} \eta^{4} + |M_{W} W_{\mu}^{+} + \frac{g}{2} \eta W_{\mu}^{+}|^{2} + \\ &+ \frac{1}{2} |\partial_{\mu} \eta + iM_{Z} Z_{\mu} + \frac{ig}{2c_{w}} \eta Z_{\mu}|^{2} - \sum_{f} \frac{g}{2} \frac{m_{f}}{M_{W}} \bar{\Psi}_{f} \Psi_{f} \eta \end{aligned}$$

$$\begin{aligned} \mathcal{L}_{\text{QCD}} &= \bar{\psi}_i \left(i \gamma^\mu (D_\mu)_{ij} - m \,\delta_{ij} \right) \psi_j - \frac{1}{4} G^a_{\mu\nu} G^{\mu\nu}_a \\ &= \bar{\psi}_i (i \gamma^\mu \partial_\mu - m) \psi_i - g G^a_\mu \bar{\psi}_i \gamma^\mu T^a_{ij} \psi_j - \frac{1}{4} G^a_{\mu\nu} G^{\mu\nu}_a \,, \end{aligned}$$





OL(arge) H(adron) C(ollider)



Large

- ~ 27km perimeter
- :: re-uses LEP tunnel

:: maximum energy depends on accelerator radius and magnitude of dipolar magnetic field that keeps particles in orbit

Hadron

protons e ions (Pb, Xe, soon O) [hadrons]

Collider

CM energy is the sum of the two beams [circulating in opposite directions]

:: advantageous wrt to fixed target and linear colliders

O detectors [the experiments]

Overall view of the LHC experiments.









ALICE 1987 people [556 authors] 41 countries





ALICE 1987 people [556 authors] 41 countries



ATLAS 6530 people [1550 authors] 45 countries







ATLAS 6530 people [1550 authors] 45 countries

CMS 5665 people [2131 authors] 57 countries





CMS 5665 people [2131 authors] 57 countries



LHCb 1499 people [947 authors] 21 countries





CMS 5665 people [2131 authors] 57 countries



LHCb 1499 people [947 authors] 21 countries

smaller experiments: FASER; TOTEM; LHCf; MoEDAL; SND@LHC
HIGGS DISCOVERY

.

Higgs production





Higgs final states

- Higgs decays [almost] instantaneously

for a light Higgs the highest decay probability

- H → b bbar [belong to jets]
- $H \rightarrow WW$
- $H \rightarrow ZZ$
- \hookrightarrow other impo
 - $H \rightarrow \gamma \gamma \gamma$
 - H → TT

H

rtant channels
excelent calorimetry]

$$\rightarrow \begin{array}{c} H \rightarrow \gamma\gamma \\ H \rightarrow WW \rightarrow e^{\mp}\nu_{e}\mu^{\pm}\nu_{\mu} \\ H \rightarrow WW \rightarrow e^{-}\bar{\nu}_{e}e^{+}\nu_{e} \\ H \rightarrow WW \rightarrow \mu^{-}\bar{\nu}_{\mu}\mu^{+}\nu_{\mu} \\ H \rightarrow ZZ \rightarrow e^{+}e^{-}e^{+}e^{-} \\ H \rightarrow ZZ \rightarrow \mu^{+}\mu^{-}\mu^{+}\mu^{-} \\ H \rightarrow ZZ \rightarrow \mu^{+}\mu^{-}e^{+}e^{-} \end{array} W$$

 $b\overline{b}$

 $F\tau\tau$ gg

0.1

WW

ZZ

 $t\bar{t}$

BR(H)

500

700

1000



pile-up

—Oa major experimental challenge is how to deal with overlapping collisions

- \hookrightarrow to increase luminosity
 - 10¹⁵ protons colliding every 50 ns (it will be 25ns soon)
 - each 'event' is the overlap of approximately 40 inelastic pp collisons



statistical significance

—Oall Higgs final states can occur as result of other SM processes [background]

- →a discovery is not made on the basis of the observation of one event, but rather as a deviation [excess] wrt to background
- statistical fluctuations of background result in local deviationsr
- probability of a given deviation being the result of a fluctuation [for gaussian background]



exclusion e look-elsewhere-effect

←→the first signal for a possible discovery is the inability to exclude

←→the ability to exclude depends on the available statistics [number of events]

-Othe larger the region [in this case of masses] you look at, the larger the probability of observing a deviation somewhere [look-elsewhere effect]

 \longrightarrow in 'delocalized' searches this has to be accounted for

this reduces the statistical significance of a local excess [magnitude of excess/ width of search region]

13 Dec 2011



13 Dec 2011



exclusion plots



- —Odashed line : without Higgs [bands of 68% and 95% CL]
- --Ofull line : ratio between cross section that is being excluded and expected SM cross section for a Higgs with a given mass

exclusion plots



exclusion plots



$\sqrt{s} = 7 \text{ TeV} \rightarrow \sqrt{s} = 8 \text{ TeV}$

:: increased production cross sections

increase of instantaneous luminosity

:: sucess in analyzing pile-up events

all particle physics analysis are 'blind' until the very end

4 Jul 2012 [dawn]



they got into the room

4 Jul 2012 [dawn]



they got into the room

they DID NOT



4 Jul 2012 [8h00]



exclusion plot







Higgs discovery in the **YY** channel



Higgs discovery in the **YY** channel



Higgs discovery in the 4l channel



Higgs discovery in the 4l channel

what has become history

Observation of a new particle in the search for the Standard Model Higgs boson with the ATLAS detector at the LHC $\stackrel{\text{\tiny{$\stackrel{l}{2}$}}}{}$

12 469 citations

ATLAS Collaboration *

This paper is dedicated to the memory of our ATLAS colleagues who did not live to see the full impact and significance of their contributions to the experiment.

ARTICLE INFO

ABSTRACT

Article history: Received 31 July 2012 Received in revised form 8 August 2012 Accepted 11 August 2012 Available online 14 August 2012 Editor: W.-D. Schlatter

A search for the Standard Model Higgs boson in proton-proton collisions with the ATLAS detector at the LHC is presented. The datasets used correspond to integrated luminosities of approximately 4.8 fb^{-1} collected at $\sqrt{s} = 7$ TeV in 2011 and 5.8 fb⁻¹ at $\sqrt{s} = 8$ TeV in 2012. Individual searches in the channels $H \to ZZ^{(*)} \to 4\ell, H \to \gamma\gamma$ and $H \to WW^{(*)} \to e\nu\mu\nu$ in the 8 TeV data are combined with previously published results of searches for $H \to ZZ^{(*)}$, $WW^{(*)}$, $b\bar{b}$ and $\tau^+\tau^-$ in the 7 TeV data and results from improved analyses of the $H \to ZZ^{(*)} \to 4\ell$ and $H \to \gamma\gamma$ channels in the 7 TeV data. Clear evidence for the production of a neutral boson with a measured mass of 126.0 ± 0.4 (stat) ±0.4 (sys) GeV is presented. This observation, which has a significance of 5.9 standard deviations, corresponding to a background fluctuation probability of 1.7×10^{-9} , is compatible with the production and decay of the Standard Model Higgs boson.

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Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC ☆

12 162 citations

CMS Collaboration *

CERN, Switzerland

This paper is dedicated to the memory of our colleagues who worked on CMS but have since passed away. In recognition of their many contributions to the achievement of this observation.

ARTICLE INFO

Article history: Received 31 July 2012 Received in revised form 9 August 2012 Accepted 11 August 2012 Available online 18 August 2012 Editor: W.-D. Schlatter

Keywords: CMS Physics Higgs

ABSTRACT

Results are presented from searches for the standard model Higgs boson in proton-proton collisions at $\sqrt{s} = 7$ and 8 TeV in the Compact Muon Solenoid experiment at the LHC, using data samples corresponding to integrated luminosities of up to 5.1 fb⁻¹ at 7 TeV and 5.3 fb⁻¹ at 8 TeV. The search is performed in five decay modes: $\gamma \gamma$, ZZ, W⁺W⁻, $\tau^+\tau^-$, and bb. An excess of events is observed above the expected background, with a local significance of 5.0 standard deviations, at a mass near 125 GeV, signalling the production of a new particle. The expected significance for a standard model Higgs boson of that mass is 5.8 standard deviations. The excess is most significant in the two decay modes with the best mass resolution, $\gamma \gamma$ and ZZ; a fit to these signals gives a mass of 125.3 ± 0.4 (stat.) ± 0.5 (syst.) GeV. The decay to two photons indicates that the new particle is a boson with spin different from one.

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Higgs theoretical paper has 'only' 6593 citations

o que vai ficar para a História



8 October 2013

The Nobel Prize in Physics 2013

The Royal Swedish Academy of Sciences has decided to award the Nobel Prize in Physics for 2013 to

François Englert

Université Libre de Bruxelles, Brussels, Belgium

Peter W. Higgs

University of Edinburgh, UK

"for the theoretical discovery of a mechanism that contributes to our understanding of the origin of mass of subatomic particles, and which recently was confirmed through the discovery of the predicted fundamental particle, by the ATLAS and CMS experiments at CERN's Large Hadron Collider"

Here, at last!

François Englert and Peter W. Higgs are jointly awarded the Nobel Prize in Physics 2013 for the theory of how particles acquire mass. In 1964, they proposed the theory independently of each other (Englert together with his now deceased colleague Robert Brout). In 2012, their ideas were confirmed by the discovery of a so called *Higgs particle* at the CERN laboratory outside Geneva in Switzerland.

The awarded theory is a central part of the Standard Model of particle physics that describes how the world is constructed. According to the Standard Model, everything, from flowers and people to stars and planets, consists of just a few building blocks: *matter particles*. These particles are governed by forces mediated by *force* Hadron Collider), is probably the largest and the most complex machine ever constructed by humans. Two research groups of some 3,000 scientists each, ATLAS and CMS, managed to extract the Higgs particle from billions of particle collisions in the LHC.

Even though it is a great achievement to have found the Higgs particle — the missing piece in the Standard Model puzzle — the Standard Model is not the final piece in the cosmic puzzle. One of the reasons for this is that the Standard Model treats certain particles, neutrinos, as being virtually massless, whereas recent studies show that they actually do have mass. Another reason is that the model only describes visible matter, which only accounts for one fifth of all matter in the



data has since become much better



the Higgs has since been discovered in multiple channels and ALL IS CONSISTENT WITH THE SM

VERY importantly we now have direct evidence for the Yukawa sector [fermion masses arising from the Higgs mechanism] :: recall that the Higgs mechanism was introduced to give masses to gauge bosons

SO WHAT?

- the Standard Model
 - unifies the electromagnetic and weak interactions [physically] and [at the formal level] the strong interaction
 - accounts for ALL experimental observations with possible hints of discrepancies [mainly in the form of violation of lepton universality :: different leptons behaving differently]
- the Standard Model does not answer many questions
 - why 3 families?
 - why are the masses what they are?
 - can electro-weak and strong forces be physically unified?
 - what is the remaining 95% of the Universe?
 - is there a higher level theory from which the SM follows? Physics beyond the SM?
 - do very appealing, and thoroughly explored, Supersymmetric theories play a role?
 - how does gravity fit in?

•

OTHER ELEPHANTS IN THE ROOM

- what is the dynamics responsible for confinement ?
 - we know how to deconfine [free quarks and gluons beyond nucleon scales] by colliding heavy nuclei
 - what is formed [quark gluon plasma] is the most perfect liquid ever observed and leads to a variety of collective behaviour patterns [emergent complexity from the simple fundamental rules of the QCD lagrangian]
 - how does the increased knowledge about the quark gluon plasma [the state of the Universe early on] affect our understanding of Cosmology?



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 - how does the increased knowledge about the quark gluon plasma [the state of the Universe early on] affect our understanding of Cosmology?
- [possibly the most intriguing thing I really care about] collective many-particle behaviour also observed in proton-proton collisions and for a small number of particles
 - is there a threshold at which collective descriptions make sense

HOW WILL WE FIND OUT [BEYOND THE LHC]





- ~100 km tunnel infrastructure in Geneva area, linked to CERN
- a broad study including:
 - FCC-ee
 - FCC-hh (pp and ions)
 - HE-LHC
 - ep/eA colliding modes
- 16 T magnets for pp@100 TeV :: PbPb@39TeV

FUTURE CIRCULAR COLLIDER [FCC] STUDY





- Concept Design Report [4 volumes] published
 - 1350 contributors from 350 institutes

